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Candidate high- z protoclusters among the *Planck* compact sources, as revealed by *Herschel*–SPIRE

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ABSTRACT

By determining the nature of all the *Planck* compact sources within 808.4 deg^2 of large *Herschel* surveys, we have identified 27 candidate protoclusters of dusty star-forming galaxies (DSFGs) that are at least 3σ overdense in either 250, 350, or 500 μm sources. We find roughly half of all the *Planck* compact sources are resolved by *Herschel* into multiple discrete objects, with the other half remaining unresolved by *Herschel*. We find a significant difference between versions of the *Planck* catalogues, with earlier releases hosting a larger fraction of candidate protoclusters and Galactic cirrus than later releases, which we ascribe to a difference in the filters used in the creation of the three catalogues. We find a surface density of DSFG candidate protoclusters of $(3.3 \pm 0.7) \times 10^{-2} \text{ sources deg}^{-2}$, in good agreement with previous similar studies. We find that a *Planck* colour selection of $S_{857}/S_{545} < 2$ works well to select candidate protoclusters, but can miss protoclusters at $z < 2$. The *Herschel* colours of individual candidate protocluster members indicate our candidate protoclusters all likely all lie at $z > 1$. Our candidate protoclusters are a factor of 5 times brighter at 353 GHz than expected from simulations, even in the most conservative estimates. Further observations are needed to confirm whether these candidate protoclusters are physical clusters, multiple protoclusters along the line of sight, or chance alignments of unassociated sources.

Key words: galaxies: clusters: general – galaxies: evolution – galaxies: starburst – submillimetre: galaxies.

1 INTRODUCTION

The formation epoch of galaxy clusters remains a poorly constrained and understood component in galaxy formation and evolutionary theories. The masses and formation time of these structures in the early universe can not only place key constraints on cosmological theories and parameters (Harrison & Coles 2011), but the elliptical galaxies in the cores of these massive clusters (Kravtsov & Borgani 2012; Ma et al. 2015) are expected to go through an intense starburst phase at $z > 2$, where a large portion of their stellar mass is rapidly built up over a time-scale $< 1 \text{ Gyr}$ (Eisenhardt et al. 2008; Hopkins et al. 2008; Petty et al. 2013; Granato et al. 2015). This starbursting phase should be visible in the far-infrared (FIR) and sub-millimetre (sub-mm), where cool dust in the galaxies re-emit absorbed ultraviolet (UV) photons. At what point this takes place

during the evolution of the cluster remains unknown, and the study and identification of clusters and protoclusters at $z > 2$ is important both for cosmology, and for understanding the evolutionary process within massive clusters and their members.

However, few clusters or protoclusters containing significant numbers of dusty starbursting galaxies have been detected and confirmed at redshift $z > 2$ (Daddi et al. 2008; Capak et al. 2011; Walter et al. 2012; Dannerbauer et al. 2014; Yuan et al. 2014; Casey et al. 2015). The rarity of protoclusters, their large luminosity distance, and lack of an X-ray detectable intracluster medium or well-formed red sequence, makes traditional cluster selection techniques ineffective at selecting clusters in the earliest stage of their evolution. The sub-mm, and to a lesser degree the FIR, benefit from a negative k -correction, enabling reasonably easy identification of sources from redshift 2 to 8, at a fixed wavelength (Blain 2002; Casey, Narayanan & Cooray 2014).

The dusty star-forming galaxies (DSFGs), are thought to play a key role in the evolution of the massive ellipticals primarily seen

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today in the cores of local clusters (Swinbank et al. 2006; Tacconi et al. 2008; Michałowski, Hjorth & Watson 2010; Stevens et al. 2010; Hickox et al. 2012; Casey, Narayanan & Cooray 2014; Toft et al. 2014; Simpson et al. 2014; Dannerbauer et al. 2014; Ma et al. 2015; Wilkinson et al. 2016). The detection of a large number of physically associated DSFGs would be surprising, as the time-scales on which they are expected to be sub-mm bright are only around 100 Myr, so detecting several physically associated sources either implies some sort of large-scale (> 1 Mpc) starburst triggering mechanism (Hung et al. 2016; Oteo et al. 2017a), or that these sources are being externally refuelled, possibly by cosmic inflows (Casey 2016; Falgarone et al. 2017).

However, several overdensities of sub-mm bright protoclusters have already been discovered (Herranz et al. 2013; Ivison et al. 2013; Clements et al. 2014; Dannerbauer et al. 2014; Casey 2016; MacKenzie et al. 2017; Oteo et al. 2016, 2017a), some of which have spectroscopic redshifts and Atacama Large Millimeter Array (ALMA) observations showing further sub-mm bright members (Ivison et al. 2013, 2016; Oteo et al. 2017a), implying that either a large-scale triggering event (> 10 Mpc) ‘activates’ the DSFGs simultaneously, or alternatively, that the duration of the starburst event is longer (0.5–0.7 Gyr, Granato et al. 2004; Lapi et al. 2011; Cai et al. 2013; Falgarone et al. 2017). Some evidence exists which suggests that the duty cycle of DSFGs in protoclusters is indeed longer than those in the field (Emonts et al. 2016; Dannerbauer et al. 2017), with depletion time-scales of several hundred Myrs. Overall however, it is uncertain which of these scenarios is correct, and the discovery and study of further protoclusters and their dusty components is needed, as measurements of the gas depletion time-scale imply the former solution is correct, whereas the surface density of sub-mm bright protoclusters implies the latter is correct. Large field and all sky surveys in the sub-mm, such as *Planck* (Tauber et al. 2010; Planck Collaboration I 2011a) or *Herschel* (Pilbratt et al. 2010), are ideal for selecting rare overdensities of DSFGs clustered together on the sky.

Negrello et al. (2005) studied the counts of extragalactic sources expected from low angular resolution surveys such as *Planck*, and concluded that several luminous IR/sub-mm sources clustered on the scale of the instrument beam may appear as an unresolved or marginally resolved source. The individual components that make up these sources could be chance projections along the line of sight, or physically associated. Therefore, many *Planck* compact objects might resolve into high- z clusters or protoclusters of dusty sources when examined with a higher resolution instrument such as the Spectral and Photometric Imaging Receiver (SPIRE) (Griffin et al. 2010) on the *Herschel* satellite.

Planck has produced three catalogues of compact sources: The early release compact source catalogue (ERCSC, Planck Collaboration VII 2011b); The Planck catalogue of compact sources (PCCS, Planck Collaboration XXVIII 2014); and the second Planck catalogue of compact sources (PCCS2, Planck Collaboration XXVI 2016a), based on 1.6, 2.6, and 5¹ full surveys of the sky. In each catalogue, the compact *Planck* sources were compiled into nine separate sub-catalogues, one for each *Planck* channel, ranging from 30 to 857 GHz. The beam sizes vary both between channel and between catalogues, but are generally around 4–5 arcmin for the 217, 353, 545, and 857 GHz channels we use here, corresponding to 2–2.5 Mpc at $z = 2$. *Herschel*–SPIRE’s 350 μ m band is matched to *Planck*’s 857 GHz channel, while SPIRE’s 500 μ m channel has

a similar wavelength and passband to *Planck*’s 545 GHz band (500 μ m against 550 μ m).

Herschel performed several wide surveys over large areas of the extragalactic sky. SPIRE operated at 250, 350, and 500 μ m, with beam full width at half-maximum (FWHMs) of 17.9, 24.2, and 35.4 arcsec, respectively.² The largest extragalactic surveys are the *Herschel*–ATLAS (H-ATLAS, 616 deg², Eales et al. 2010), the *Herschel* multi-tiered extragalactic survey (HerMES, including the HerMES large mode survey (HeLMS), ~ 370 deg²; Oliver et al. 2010, 2012) and the *Herschel* Stripe 82 survey (HerS, 79 deg²; Viero et al. 2014). This provides over 1000 deg² of sky with approximate flux density 1σ limits of 7–10 mJy in the three SPIRE bands. By cross-matching the higher resolution *Herschel* map with the catalogues of *Planck* sources, the nature of all the *Planck* compact sources in the *Herschel* fields can be determined.

Several authors have already found plausible high-redshift clusters using the *Planck* data (Herranz et al. 2013; Clements et al. 2014; Baes et al. 2014; Planck Collaboration XXVII 2015; Planck Collaboration XXXIX 2016d; Kato et al. 2016), with a variety of approaches. Both Herranz et al. (2013) and Clements et al. (2014) performed similar cross-matches between *Herschel* and *Planck* in order to search for clusters of DSFGs. Herranz et al. (2013) used 134 deg² of preliminary H-ATLAS Phase 1 data and the ERCSC and discovered a redshift 3.26 candidate cluster/protocluster of sub-mm sources surrounding the lensed source H12-00 (Fu et al. 2012; Clements et al. 2016). Clements et al. (2014) meanwhile, cross-matched the ERCSC with the HerMES survey, and found evidence for four further candidate protoclusters of DSFGs, with each candidate protocluster having total star formation rates (SFRs) $> 1000 M_{\odot} \text{ yr}^{-1}$.

Here, we set out to investigate and characterize the nature of all the *Planck* compact sources that fall within any of the major *Herschel* fields, using H-ATLAS, HerMES, and HerS, with the aim of searching for further rare cluster/protocluster candidates and potentially other rare and unexpected sources. In general, since we are unable to confirm whether our detected clusters/protoclusters contain a well-developed intracluster medium, and since they generally span scales on the order of arcminutes, we will refer to them as protoclusters rather than clusters unless otherwise stated. This is prudent given our uncertainties about the evolutionary state of these systems, but we do allow for the possibility that some of our protoclusters are actually physically evolved clusters.

The rest of this paper is organized as follows: in Section 2, we describe the data sets used in this paper. In Section 3, we outline the methodology used to cross-match with *Herschel*, and present the matches we found between *Planck* and *Herschel*. In Section 4, we verify the photometry of our sources from the *Planck* and *Herschel* observations. In Section 5, we examine the colours of the *Planck*-detected sources, and discuss the likely nature of the reddest sources discovered, whilst in Section 6, we further characterize our candidate protoclusters. In Sections 7 and 8, we discuss the implications of our findings and summarize our results. Throughout this paper, we assume a standard cosmology, with $H_0 = 67.7 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_M = 0.3$, and $\Omega_{\Lambda} = 0.7$.

2 DATA SETS

In this section, we provide a brief overview of the construction of the three *Planck* and 17 *Herschel* catalogues used in this paper, as

¹ For the highest frequency channels only.

² SPIRE Handbook, Version 3.1, 2017 February 8, http://herschel.esac.esa.int/Docs/SPIRE/spire_handbook.pdf.

Table 1. The 17 *Planck*/*Herschel* fields under consideration in this paper, their areas, and the number of unique *Planck* sources detected within them across all three compact source catalogues.

Field	Area (deg ²)	<i>Planck</i> source count	
		857 GHz	545 GHz
NGP	170.0	82	21
SGP	285.0	91	35
GAMA09	53.4	26	13
GAMA12	53.6	15	5
GAMA15	54.6	16	13
ADFS	7.5	3	3
BOOTES	11.3	11	2
CDFS-SWIRE	10.9	5	1
COSMOS HerMES	4.4	2	1
EGS HerMES	2.7	1	0
ELAIS N1 SWIRE	12.3	6	2
ELAIS S1 SWIRE	7.9	2	0
FLS	6.7	5	3
GOODS-North	13.5	0	0
LOCKMAN-SWIRE	16.1	6	3
XMM-LSS-SWIRE	18.9	4	2
HerS	79.0	38	14
Total	808.4	313	118

well as the limits of each catalogue and any key differences between them. A summary of the *Herschel* field properties is given in Table 1, and a map of their location on the sky is given in Fig. 1.

2.1 The *Planck* compact catalogues of sources

The ERCSC used *SEXTRACTOR* (Bertin & Arnouts 1996) on the *Planck* maps to identify sources in each band; this is based on extracting a number of connected bright pixels that are some threshold above a background measurement. The PCCS and PCCS2, on the other hand, divided the maps into multiple patches, and convolved these patches with a second-order Mexican-hat wavelet that had been locally optimized to detect point sources (López-Cañiego et al. 2006). Peaks $>5\sigma$ in the resulting convolved map were then classified as detections (Planck Collaboration XXVIII 2014).

We focus on the High Frequency Instrument’s (HFI) 857 GHz (350 μm) and 545 GHz (550 μm) channels (Lamarre et al. 2010), since the rest-frame peak of dust emission in galaxies (around 100 μm) will be redshifted into these bands between $z = 1$ and 5. The quoted FWHM beam size varies between catalogue releases, between 4.23 and 4.63 arcmin in the 857 GHz band, and between 4.47 and 4.83 in the 545 GHz band due to improvements in calibration and beam information (Planck Collaboration XXVI 2016a). The 90 per cent flux completeness level for the 857 GHz band is given as 680 and 790 mJy³ at Galactic latitudes $|b| > 30^\circ$ for the PCCS and PCCS2 respectively. The ERCSC does not provide a 90 per cent completeness level, but the faintest source detected at $|b| > 30^\circ$ is 655 mJy, with the flux density of the faintest 10σ source at $|b| > 30^\circ$ being 813 mJy, demonstrating that the limits of the three catalogues at 857 GHz are all typically around 700–800 mJy. We use the aperture photometry flux density estimate in the *Planck* catalogues, as it performs best when compared to *Herschel* (see Table 12 of Planck Collaboration XXVI 2016a), is likely to correctly cap-

ture emission from extended structures, and is available in all three catalogues.

2.2 H-ATLAS

H-ATLAS surveyed five fields: The Northern Galactic Pole (NGP, 170 deg²), the Southern Galactic Pole (SGP 285 deg²), and three smaller fields that lie along the equatorial plane at RAs of approximately 9^h, 12^h, and 15^h referred to as GAMA09, GAMA12, and GAMA15 (around 54 deg² each) which correspond to three of the fields surveyed by the Galaxy and Mass Assembly (GAMA) project (Driver et al. 2011). Maps were produced with the *Herschel* Interactive Pipeline Environment (HIPE) (Ott, Centre & Agency 2010), and the typical 1σ total noise per *Herschel* beam (confusion plus instrumental) in the final background-subtracted and filtered maps is 7.4, 9.4, and 10.2 mJy for the 250, 350, and 500 μm bands, respectively (Valiante et al. 2016, Maddox et al., in preparation, Smith et al., in preparation). Sources were extracted using the Multi-band Algorithm for source detection and extraction (*MADX*) (Maddox, in preparation).

2.3 HerMES

HerMES field sizes varied from 0.4 deg² for GOODS-North, up to 280 deg² for the HeLMS field. The majority of the fields have 1σ total noises of 6.2–6.8, 7.1–7.5, and 8.2–8.9 mJy for the 250, 350, and 500 μm bands, respectively, with the exception of FLS, ADFS, ELAIS-N1, ELAIS-S1, BOOTES, and XMM-LSS, which have 1σ noise levels of 7.9, 8.2, and 10.1 mJy (Nguyen et al. 2010). We exclude the HeLMS field from further study, since no publicly released, formally verified catalogue of detected sources is yet available for cross-matching, and the field is strongly contaminated with Galactic cirrus. We do examine the *Planck* compact sources present in HeLMS using a private catalogue in Section 7, but do not include them in our final results. The maps used in this paper were produced using the SPIRE–HerMES Iterative Mapper (Levenson et al. 2010), and the catalogues we used were the DR4 xID250 catalogues (Wang et al. 2013).

2.4 HerS

The HerS (Viero et al. 2014) is a 79 deg² survey taken along the Sloan Digital Sky Survey (SDSS) Stripe 82 region with the SPIRE instrument on *Herschel*. Sources were extracted from the 250 μm map using *STARFINDER* requiring $S/N > 3$, after filtering the maps with a high-pass filter to remove extended emission. Flux estimates were then extracted from the 350 and 500 μm maps, using the 250 μm source positions as a prior. The 1σ median total noise is 7.1, 7.1, and 8.4 mJy for the 250, 350, and 500 μm bands, respectively.

3 SELECTION METHODS

At 857 and 545 GHz, the *Planck* beam physically corresponds to a size of a few hundred kpc at a redshift of 0.1, and around 2.5 Mpc at redshifts 1–3. Therefore, most sources will not be resolved in the *Planck* maps, since only local ($z \ll 1$) extragalactic sources, extended Galactic cirrus, or galaxy clusters larger than 2.5 Mpc could have emission extended on larger angular scales. By visually inspecting the *Herschel* maps at the positions of the *Planck* sources, the nature of the *Planck* sources in these regions can be studied.

³ This is higher than for the PCCS (see section 3.2.3 of Planck Collaboration XXVI 2016a).

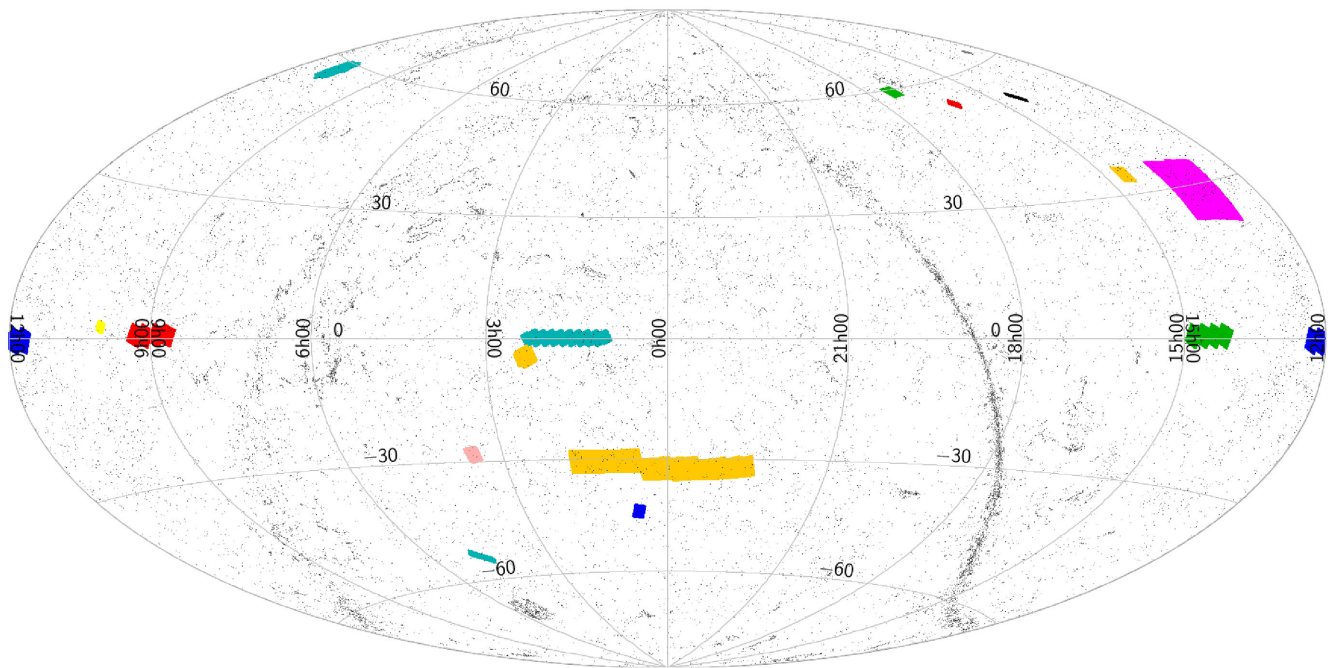


Figure 1. All-sky map showing the 17 *Herschel* fields under examination here (coloured polygons) and all 38 260 *Planck* compact sources (black dots). Some of the major fields include the NGP (magenta, Dec. of 30°), the SGP (yellow, Dec. of -30°), HerS (turquoise, centre), and the three GAMA fields centred at a Dec. of 0° and RA of 09^h (red), 12^h (blue), and 15^h (green). The Milky Way is indicated by the thick band of *Planck* sources stretching across the sky.

3.1 Creation of the *Planck*–*Herschel* catalogue

As different detection pipelines used in the creation of the ERCSC, PCCS, and PCCS2 could be sensitive to different source populations, we include all three as part of our analysis. We cross-match each *Planck* catalogue with the 17 catalogues of *Herschel* sources. We use a search radius equal to the *Planck* FWHM at 857 GHz in the PCCS2, which used the most up to date calibration and beam information (4.63 arcmin). We varied this search radius between 4.00 and 5.00 arcmin to check for consistency, as the *Planck* beam FWHM varies not only with channel, but also with *Planck* catalogue, typically between 4.2 and 4.8 arcmin. With the exception of some minor changes in the number of *Herschel* sources detected in each *Planck* source, our conclusions remained consistent. The *Herschel* source density is high enough that there are always multiple *Herschel* sources per *Planck* beam, typically >10 . For the 857 GHz – 350 μm match, there are 160 *Planck* sources in the *Herschel* fields from the ERCSC, 229 from the PCCS, and 168 from the PCCS2. The 545 GHz – 500 μm match finds 50 *Planck* sources from the ERCSC, 99 from the PCCS, and 60 from the PCCS2.

In Fig. 2, we plot the aperture flux values for our *Planck* sources. While the PCCS and PCCS2 appear to be similar in terms of their flux distribution, the ERCSC distribution is skewed towards higher flux values. The ERCSC, using *SEXTRACTOR*, requires isolated, bright, connected pixels in order to flag a detection, with the minimum flux found for the whole ERCSC being 655 mJy at 857 GHz. The PCCS and PCCS2, on the other hand, require a single local peak in the *Planck* map after convolution with the filter, and so can contain $>5\sigma$ sources with aperture fluxes as low as 69 mJy in our catalogue. However, for bright sources detected in all three catalogues, the distributions should be similar, and above an aperture flux of ~ 750 mJy, we find a much better match between the source flux densities.

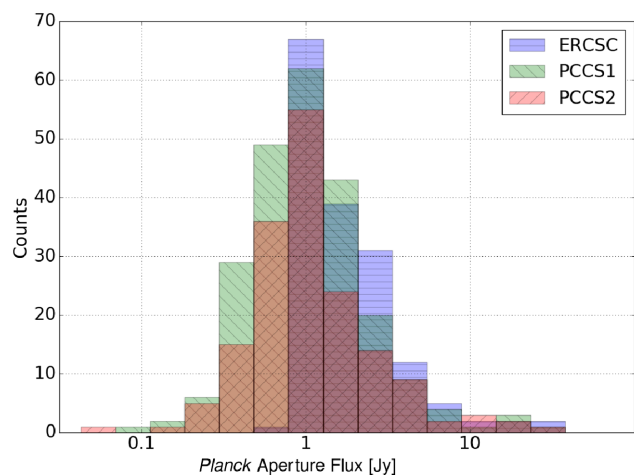


Figure 2. Aperture flux distribution of *Planck* sources that lie in one of our *Herschel* fields from the ERCSC (blue), PCCS (green), and PCCS2 (red).

Cross-matching the three versions of the catalogues together to find the total number of *Planck* compact sources detected in at least one of the three catalogues, we find 313 unique *Planck* sources in the *Herschel* fields from the 857 GHz band and 118 unique *Planck* sources from the 545 GHz band. Combining these two catalogues together to search for unique objects, we find a total of 354 sources detected across 808.4 deg^2 .

We also create a catalogue of *Herschel* sources that fall within 4.63 arcmin of each *Planck* source. We created two uniform catalogues of *Herschel* sources for the 857 and 545 GHz data by selecting *Herschel* sources using a minimum flux density limit of 25.4 mJy at least 25.4 mJy in its respective SPIRE band (i.e. for

Table 2. Identifications of all the *Planck* objects that fall within one of the *Herschel* survey fields under consideration here.

Type	857 GHz	545 GHz	Unique
Local galaxies	187	54	192
Galactic cirrus	37	18	43
Protocluster candidates	21	10	27
Lensed sources	12	2	12
Stars	3	2	3
QSOs	2	1	2
Off map	13	3	14
No assignment given	38	28	61
Total	313	118	354

a *Planck* source detected at 857 GHz, a *Herschel*–SPIRE source needs to be at least 25.4 mJy in the SPIRE 350 μ m band). This is approximately three times the highest median total error seen in any of the *Herschel* fields. This results in 3709 individual sources with $S_{350} > 25.4$ mJy ($\gtrsim 3\sigma$) that lie within 4.63 arcmin of a *Planck* 857 GHz source, and 736 *Herschel* sources with $S_{500} > 25.4$ mJy that lie within 4.63 arcmin of a *Planck* 545 GHz source.

Finally, we cross-matched our catalogue of unique compact *Planck* objects with the *Planck* Sunyaev–Zel’dovich Galaxy Cluster Catalogue (SZ, Planck Collaboration XXVII 2016b), the *Planck* Galactic cold clump catalogue (Planck Collaboration XXVIII 2016c), and the *Planck* High Z catalogue (PHZ, Planck Collaboration XXXIX 2016d). We found no matches with the SZ catalogue, a single match with the Galactic cold cores catalogue, PLCK-ERC857 G339.76–85.56, and four matches in the PHZ, PCCS1 545 G160.59–56.75, PCCS1 545 G084.81+46.34, PLCKERC545 G007.56–64.14, and PCCS1 545 G012.89–66.24.

3.2 The nature of the *Planck* sources

We visually inspected each source in the *Herschel* 350 μ m maps at the position of the *Planck* objects, to identify the nature of each *Planck* source. A summary of our results is presented in Table 2, a table containing our candidate clusters is available in Appendix B, a table containing all our sources is available online, and images of the 324 that lie on the maps and away from the edge are available in Appendix A.

Most local ($z \ll 1$) galaxies can be identified by their bright, point source or extended emission in the *Herschel* maps. Cross-matching these with the NASA Extragalactic Database (NED) identifies 192 local galaxies, two quasi stellar objects (QSOs), and eight lens candidates that have known H-ATLAS identifications. Four times, single bright sources with $S_{350} > 50$ mJy are found to have no optical or other known counterparts in NED or elsewhere. These we assign as additional lens candidates, though these could also easily be examples of hyperluminous infrared galaxies, with $L_{\text{fIR}} > 10^{13} L_{\odot}$, and are not necessarily lensed. Sources were also cross-matched with SIMBAD (Wenger et al. 2000), and three stars were identified this way. Fourteen of the *Planck* sources lie just outside the map coverage, and these are included in Table 2 but not considered further.

For the remaining 131 sources, as well as examining the *Herschel* maps, we examined the (IRIS, Miville Deschenes & Lagache 2005) maps at the positions of the *Planck* sources to search for bright emission at 100 μ m, which will be present for Galactic cirrus but not for protoclusters of DSFGs at redshifts $\gtrsim 1$. *Planck* objects with structures in the 100 μ m map IRIS maps were conservatively cat-

egorized as Galactic cirrus, 43 in total. This left 88 regions without an identification.

To search for protoclusters amongst these 88, we counted the number of 250, 350, and 500 μ m sources with fluxes > 25.4 mJy that lie within 4.63 arcmin of the *Planck* position, with the flux limit chosen to compare to published number counts. Assuming our sources are Poisson distributed, number counts from Clements et al. (2010) and Valiante et al. (2016) suggest that the expected number of 250, 350, and 500 μ m sources are 16.5 ± 4.1 , 9.1 ± 3.0 , and 2.7 ± 1.7 per *Planck* beam. Any objects that show a 3σ overdensity in any of the three SPIRE bands (at least 31, 19, or 9 sources⁴ in the 250, 350, or 500 μ m bands, respectively) are classed as candidate protoclusters of galaxies, 27 in total are found in this way. These overdensities are not necessarily physical associated protoclusters, as they could also be line-of-sight effects of unrelated sources, multiple clusters/protoclusters along the same line of sight (Flores-Cacho et al. 2016; Negrello et al. 2016), or they might be explained by differences in the actual distributions of the number of *Herschel* sources in the tail of the distribution compared to Poisson. The assumption of Poisson oversimplifies the complex distribution of galaxies, so in order to justify our assumption, we simulate 10 000 *Planck* beams (circles of radius 4.63 arcmin) at random positions on the NGP 350 μ m map, and count the number of *Herschel* sources with $S_{350} > 25.4$ mJy. We then compare this to our Poisson assumption that 19 or more sources indicates an overdensity. Only 16 of 10 000 of the random positions contain at least 19 *Herschel* sources with $S_{350} > 25.4$ mJy, with an average of 8.8 ± 2.9 per *Planck* beam, in good agreement with the estimates from Valiante et al. (2016). Interpreting the 16 out of 10 000 as a probability, and converting this to an equivalent σ value in the normal distribution, this corresponds to a 2.94σ overdensity, in excellent agreement with our choice of assuming these sources are Poisson distributed. We find similar results for the 250 and 500 μ m bands. Therefore, these 27 *Planck* sources are clearly overdense in *Herschel* sources, and we assign them as candidate protoclusters, though we retain the possibility that these are line-of-sight effects or multiple clusters/protoclusters along the line of sight. The remaining 61 sources in our maps remain unclassified, as we cannot reliably determine their nature. We thus have a total of 340 unique *Planck* compact sources across both the 857 and 545 GHz bands, including local galaxies, Galactic cirrus, protocluster candidates, lensed sources, stars, and QSO’s sources we were unable to assign a classification.

3.3 Properties of our catalogues

3.3.1 Nature of the unassigned sources

We cannot reliably assign a category for several of our sources. These could be false detections by *Planck* or a series of fainter sources which we do not detect in *Herschel*. Significant differences at low signal-to-noise ratio (S/N) were seen from preliminary versions of the catalogues, which were created from preliminary versions of the *Planck* maps (Harrison, private communication). Keeping the parameters for the *Planck* catalogue creation the same, sources near the detection threshold would appear/disappear, depending on the preliminary version of the map used in the creation of the *Planck* catalogue. For sources detected at a high S/N, this was very rare, whilst for sources near the detection thresholds, this was more common.

⁴ Using Poisson statistics.

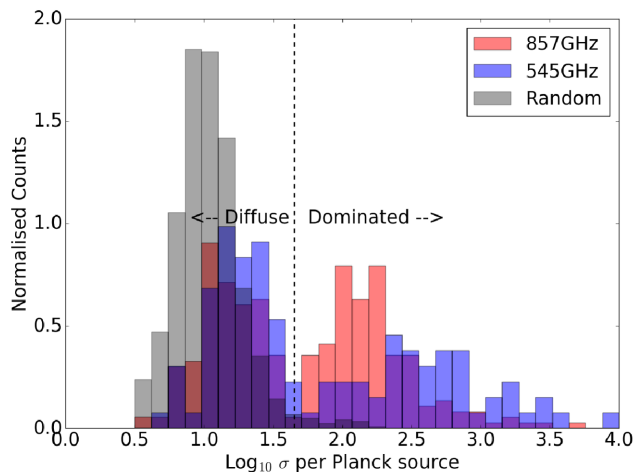


Figure 3. Log of the dispersion at 350 μm for the *Herschel* sources contained within a *Planck* object in the 857 (red) and the 545 (blue) GHz catalogues. The vertical black dashed line indicates the selected division between ‘diffuse’ and ‘dominated’ sources. In grey is the result from taking 1000 random positions in the NGP field, showing very few sources in the ‘dominated’ region.

In our catalogue, for sources not assigned a counterpart, the median detection level in the PCCS and PCCS2 is $5.4 \pm 0.5\sigma$, near the detection threshold of 5σ (for our protoclusters, this is similar at $5.4 \pm 0.3\sigma$). However, 10 of the 65 are detected in multiple catalogues (six of these were detected in both the ERCSC and either the PCCS or PCCS2, thus using different detection methods). This is unlikely if these 10 sources are false detections. Of these 10, five have colours that would be selected as a high-redshift candidate by the PHZ in their analysis of candidate high- z sources in *Planck* (Planck Collaboration XXXIX 2016d). This could indicate an overdensity of red compact sources, too faint to be included in our analysis. This conclusion was also hinted at when varying our search radius between 4.00 and 5.00 arcmin; several of our unassigned sources became classified as candidate protoclusters, and several candidate protoclusters became unassigned. In all cases, we found roughly 30 candidate protoclusters, with the exact number depending both on our choice of search radius, and flux density limit. It is therefore likely that some of the unassigned sources are protoclusters of DSFGs, but for the specific values we have chosen they do not pass our threshold test.

3.3.2 Diffuse and dominated sources

Given we are searching for protoclusters, we take all the *Herschel* sources associated with a *Planck* 857 GHz object, and calculate the standard deviation of their *Herschel* 350 μm flux densities, σ_{350} . A large value of σ_{350} is likely due to singular bright sources, whereas a small value indicates either of multiple distinct sources as in a protocluster, or simply extended Galactic cirrus. We do the same for the 545 GHz *Planck* sources and the *Herschel* 500 μm flux densities, σ_{500} . We show these in Fig. 3 for all 340 *Planck* objects, as well as the result when taking 1000 random positions, and calculating the log σ_{350} in each case as a comparison. Any source with fewer than two *Herschel* sources is not included in our analysis. There are 28 sources with 2, 3, or 4 associated 350 μm detections, so the vast majority have reasonable samples from which to calculate σ_{350} . The distribution appears bimodal, with two distinct regions below and above $\log_{10}(\sigma) \approx 1.65$. This bimodality is not seen when

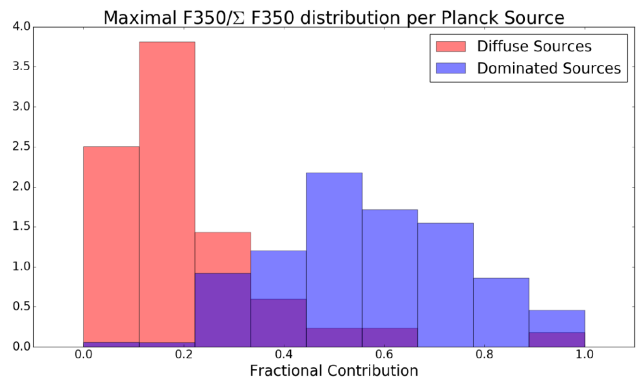


Figure 4. Fractional contribution of the brightest *Herschel* source in each *Planck* source to the total *Herschel* 350 μm flux density from all the sources associated with each *Planck* object. ‘Diffuse’ sources (red) and ‘dominated’ sources (blue) are plotted separately.

examining 1000 random positions. We designate these two regions as ‘diffuse’ ($\log_{10}(\sigma) < 1.65$) and ‘dominated’ ($\log_{10}(\sigma) > 1.65$), indicating that flux from these sources appears to be from extended diffuse/multiple faint source emission or dominated by a single source, respectively.

For the 857 GHz *Planck* sources, of the 299 sources not near the edge and with more than one associated *Herschel* sources, 155 sources are identified as ‘dominated’ and 144 are identified as ‘diffuse’. In the 545 GHz catalogue, of the 109 sources not near the edge and with more than 1 associated *Herschel* sources, 44 are ‘dominated’ and 65 are ‘diffuse’. Overall this resulted in 159 unique ‘dominated’ sources and 186 unique ‘diffuse’ sources, with nine sources having only one counterpart or lying near the edge of the *Herschel* map. All the cirrus sources, all the protocluster candidates and all but one of the not assigned sources are identified as being ‘diffuse’. The other 156 ‘dominated’ sources are all identified with local galaxies, lensed candidates, the QSO, or stars. Of the 186 total ‘diffuse’ sources, 41 are associated with local galaxies, usually because of extended emission or several bright neighbours. We also find that four of the lens sources are diffuse, though they lie on the border between diffuse and dominated.

In Fig. 4, we plot the distribution of the fractional contribution from the brightest 350 μm *Herschel* source to each *Planck* 857 GHz source, divided by whether a *Planck* source is ‘diffuse’ or ‘dominated’. This independently shows that our intuitive explanation for the division seen in the σ_{350} seems to be the correct one; ‘dominated’ objects tend to have one bright source dominating the flux whereas the ‘diffuse’ objects individually have a relatively low contribution to the total flux. A similar relationship is seen in the 545 GHz data.

The clear divide in both Figs 3 and 4 indicates that only around 60 per cent of the *Planck* compact sources are actually compact on scales reasonably smaller than the *Planck* beam. Both figures also show that the *Planck* maps are well suited for detecting extended emission from sources such as protoclusters of DSFGs.

3.3.3 Variations between the ERCSC, PCCS, and PCCS2

The key difference between the *Planck* compact source catalogues is the use of SEXTRACTOR for the ERCSC and a Mexican-hat wavelet for the detection pipeline in the PCCS and PCCS2. This latter approach was designed to suppress emission on large scales, in order to reduce cirrus contamination in the catalogues, and simulations of its effectiveness were run on point sources (López-Caniego et al.

Table 3. Fractional make up of the three *Planck* catalogues of compact sources at 857 GHz.

Source type	ERCSC (per cent)	PCCS (per cent)	PCCS2 (per cent)
Local galaxies	56.0	61.0	80.0
Galactic cirrus	16.7	8.8	5.0
Cluster candidates	9.5	4.6	1.1
No assignment given	11.9	16.1	5.6
Lenses	1.2	3.8	3.3
QSO	0.0	0.8	0.5
Stars	0.6	1.1	1.7

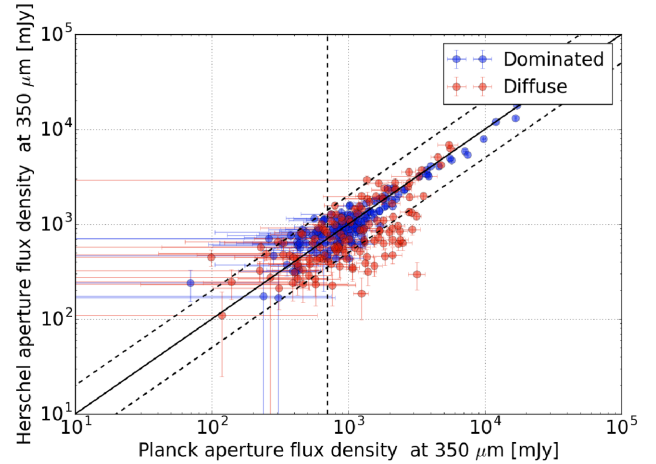
2006). However, its effect on extended, non-cirrus sources is unclear.

In Table 3, we provide the fractional composition of each 857 GHz catalogue. Though from the ERCSC to the PCCS2, the cirrus contamination of the catalogues has reduced from 16.7 per cent to 5.0 per cent, the fraction of protocluster candidates has been also reduced from 9.5 per cent to 1.1 per cent. Put another way, the fraction of ‘diffuse’ sources has decreased from ~ 47 per cent in the ERCSC to 28 per cent in the PCCS2. Though these protocluster candidates may not be real, may be line-of-sight effects, or potentially cirrus contamination, recent work has shown that several of these candidates are consistent with their being clusters in formation at $z \sim 2$ (Herranz et al. 2013; Clements et al. 2014, 2016, Cheng et al., in preparation). The inclusion of the Mexican-hat wavelet for source detection potentially suppresses the detection of these protocluster candidates, as the BOOTES, Extended Groth Strip (EGS), Lockman, and Chandra Deep Field South (CDFS) protocluster candidates revealed by Clements et al. (2014) do not appear in the PCCS or PCCS2.

4 PHOTOMETRY

Having identified our 27 protocluster candidates, alongside numerous other source types, we now examine the photometry associated with these sources. *Planck* have previously compared their photometry against *Herschel* in order to verify that the two photometry measurements agree (Bertincourt et al. 2016). In this section, we extend this analysis to checking whether summing our selected 350 μm *Herschel* sources (i.e. $S_{350} > 25.4$ mJy) alone can adequately match the *Planck* flux densities seen in all the *Planck* compact sources.

As the band passes are well matched, a direct comparison between the 857 GHz *Planck* band and the 350 μm SPIRE band can be performed with few assumptions. Here, we follow the same procedure set out in appendix A.1 of the PCCS for estimating the aperture photometry, but use the *Herschel* maps instead of the *Planck* maps. We took the background subtracted maps of all of the *Herschel* fields, and integrated the SPIRE 350 μm flux density over a *Planck* 857 GHz beam by summing all the pixels that fell within 1 FWHM of the nominal *Planck* source position. The assumed FWHM was 4.63 arcmin. Once again, this was varied between 4.0 and 5.0 arcmin to check for consistency in the results, finding similar results. The background annulus of inner radius $1 \times \text{FWHM}$ and outer radius of $2 \times \text{FWHM}$ was used to estimate the median background value

**Figure 5.** Comparison between the *Planck* aperture flux density and the *Herschel* aperture flux density, as calculated in the text. The red points are the those sources considered to be diffuse, and the blue those considered dominated by a single source. The solid black line shows the 1:1 ratio. The diagonal dashed lines show the limits where the *Herschel* flux is half/double that of the *Planck* flux, and the vertical dashed line shows the PCCS 90 per cent completeness limit.

and this was removed from the aperture flux estimate. Any sources that fell on the edge of the map or contained null pixels within the primary or background aperture had a flux density assigned to them of zero to prevent edge effects contaminating our sample. Errors were estimated from a combination of SPIRE instrumental noise, SPIRE calibration error, and a constant confusion noise conservatively estimated at 7 mJy per SPIRE beam, all added in quadrature. The results of this analysis, for both diffuse and dominated sources, are shown in Fig. 5.

We then use the absolute relative flux density difference, defined as

$$\eta = |100 \times \frac{S_{\text{SPIRE}} - S_{\text{Planck}}}{S_{\text{SPIRE}}}|, \quad (1)$$

where S_{SPIRE} gives the *Herschel* aperture flux density, as integrated over a *Planck* beam, and S_{Planck} is the quoted *Planck* aperture flux density immediately after the equation and use the weighted average of the *Planck* and *Herschel* aperture photometries, finding an absolute relative flux density difference between *Planck* and *Herschel* of only 4.9 per cent, comparable to the 1–5 per cent uncertainty found in Bertincourt et al. (2016).

The absolute relative flux density difference is, however, not the same for the dominated (1.8 per cent) and diffuse (11.4 per cent) sources. Given we are using background subtracted maps in each case, we repeat our analysis using the raw H-ATLAS maps that are publicly available. These *Herschel* maps have not had any background subtraction applied to them, and therefore could contain the flux that appears to be missing in several of our diffuse sources for *Herschel*. We found that absolute relative flux density difference for our dominated and diffuse sources changed to 4.8 per cent and 3.8 per cent, respectively, when we used the raw maps, both well within the *Planck* calibration uncertainty. This indicates that the missing flux from our sources, especially diffuse sources, is being removed during the background removal process on the *Herschel* maps.

The *Planck* and *Herschel* aperture photometries are generally in agreement for *Planck* objects dominated by a single *Herschel*

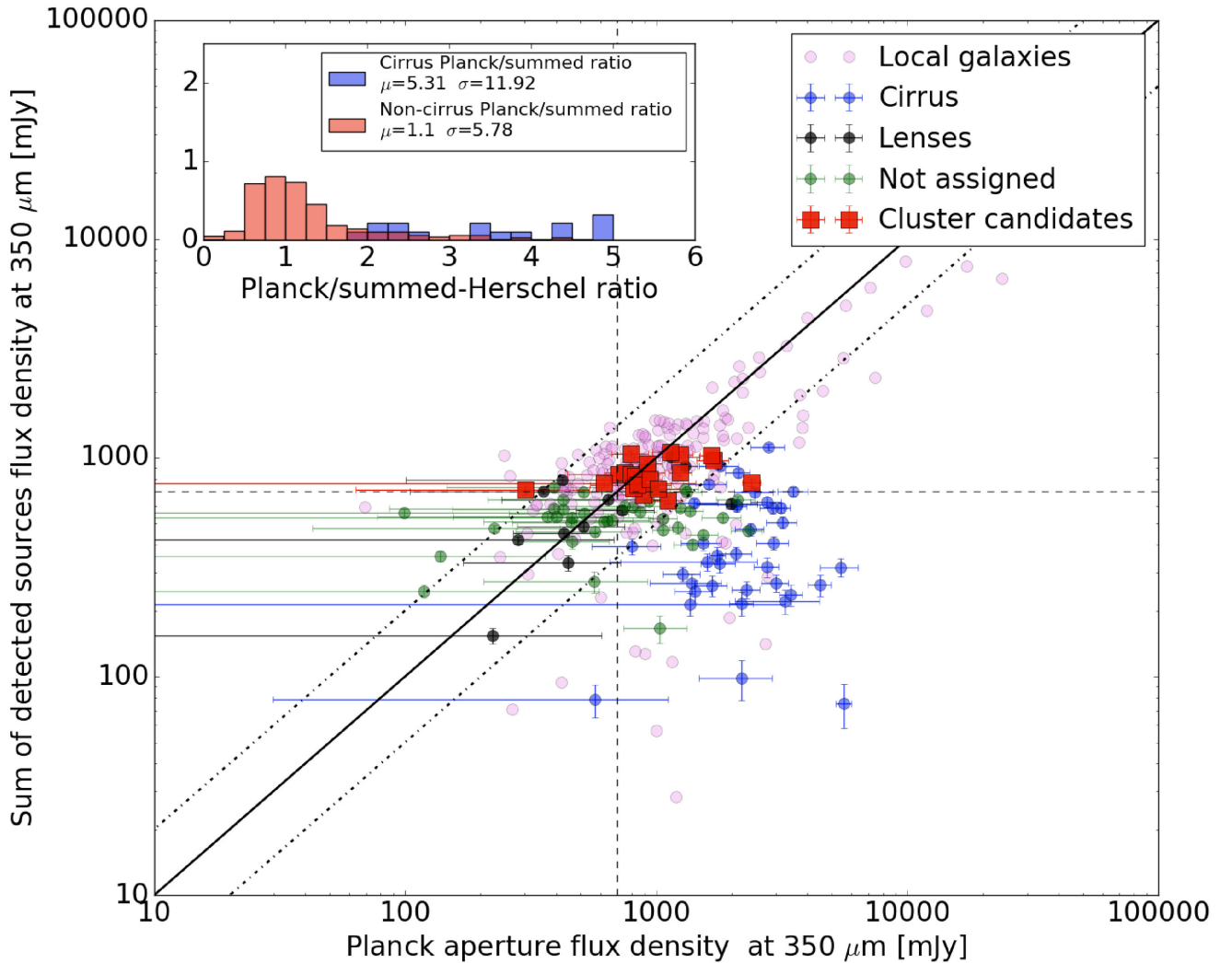


Figure 6. Comparison between the *Planck* aperture flux density and summing up the 350 μm flux density from the detected *Herschel* sources. The light pink points are local galaxies, the blue are Galactic cirrus, the red are protocluster candidates, the black are lens candidates, and the green are those points not assigned an identification. The solid black line shows the 1:1 ratio, whereas the dot-dashed lines show where the *Planck* aperture flux is double or half the summed detected sources. The vertical and horizontal dashed lines show the nominal *Planck* 90 per cent completeness levels from the PCCS. Error bars are not shown for the local galaxies to aid in clarity, but are comparable to other sources at all fluxes. The histogram in the top left corner shows the *Herschel* *Planck* ratio, with cirrus sources indicated in blue, and non-cirrus sources indicated in red, as well as the mean and standard deviation. The histogram has been truncated to a maximum ratio of 6 for clarity, with 19 cirrus sources with ratios beyond this.

source. Given roughly 40 per cent of all *Planck* compact objects are expected to be diffuse in nature when examined at *Herschel* resolutions, we consider whether the detected *Herschel* sources alone can account for the total *Planck* flux, or whether an extended diffuse emission component is required.

In Fig. 6, we plot the *Planck* aperture flux densities and the summed 350 μm fluxes from the detected *Herschel* sources, coloured by their source classification type. We find a 5 per cent absolute relative flux density difference between the summed fluxes and the aperture flux for non-cirrus sources, but a 77 per cent relative flux difference for sources we have identified with Galactic cirrus. Several local galaxies, with emission extended well beyond the scale of the *Herschel* beam, are poorly fit in the *Herschel* catalogues and therefore have a smaller summed-*Herschel* flux compared to the *Planck* flux.

When summing up detected *Herschel* sources, protocluster candidates are well matched to *Planck* but Galactic cirrus sources are

not, suggesting that our selection of Cirrus sources in Section 3 was successful. This also implies that estimates of the physical properties of these protocluster candidates can be derived from the *Planck* flux density alone, as it represents the summed total of the individual sources that make up the protocluster and no diffuse emission is needed to account for the *Planck* flux.

Fig. 6 also shows that the protocluster candidates mostly lie near to the *Planck* detection limits, with a median *Planck* aperture flux of 886 mJy. Only eight of our 21 candidate protoclusters detected at 857 GHz have an 857 GHz flux density > 1 Jy. For the unassigned objects, 14 of 63 have *Planck* 857 GHz flux densities > 1 Jy, and these brighter sources we often find are not well matched between *Planck* and *Herschel*; only two of these unassigned sources have *Herschel* aperture flux densities > 1 Jy, and none of the unassigned sources have a 857 GHz flux density > 1 Jy when summing detected *Herschel* sources. Given also that Fig. 2 indicates the ERCSC, which appears to be best at detecting these protocluster candidates,

is limited to sources with flux density >750 mJy, it is possible that the candidates we are selecting here are the bright tail of the DSFG protocluster population, and there could be many more protoclusters that lie below this limit.

5 COLOURS

With only a maximum of three photometric points from SPIRE available, any photometric redshift attempt will have large uncertainties ($\Delta z = \pm 1$) associated with it. However, the sub-mm colours of *Herschel* sources have often been used as a proxy to give a useful indication of their redshifts (Clements et al. 2014; Dowell et al. 2014; Dannerbauer et al. 2014; Asboth et al. 2016; Rowan-Robinson et al. 2016; Ivison et al. 2016). Therefore, in this section we set out to examine the *Planck* colours of our sources, and compare them to the selection used by the PHZ in their search for high- z sources, as well as using the *Herschel* colours to give an indication of the likely redshifts of our *Planck* sources. We leave a more accurate determination of the redshift to a future paper that contains additional follow up observations (Cheng et al., in preparation).

5.1 *Planck* colours

In Fig. 7, we plot the *Planck* 857/545 GHz (350/550 μ m) and 545/353 GHz (550/850 μ m) colours for the major populations identified in Section 3.2. We only plot sources from the 857 GHz selected catalogue, since it is the only catalogue which additionally provides aperture flux estimates at 545 and 353 GHz at the position of the *Planck* source. Planck Collaboration XXXIX (2016d), in their selection of high- z candidates from the *Planck* maps, used a criterion with *Planck* colours of 857/545 GHz < 2 and 545/353 GHz > 1 to search for candidate high-redshift galaxies/clusters of galaxies. We mark their selection area as the grey hashed region. For clarity, only the local galaxies that are detected at 3σ in all three of the 857, 545, and 353 GHz bands are plotted. We also plot two of the protoclusters detected by Clements et al. (2014) in the BOOTES and EGS fields to demonstrate their colours (both of which are also detected in our analysis).

We note that many of our protocluster candidates fall outside the *Planck* selection region. For our identified candidate protoclusters, 21 are included in the 857 GHz *Planck* catalogue, and so are considered here. Of these 21, only 12 lie within the *Planck* selection region, with a mean S_{857}/S_{545} ratio of 2.0 ± 0.5 . As the only constraint we impose upon our sources is that they are detected as a *Planck* compact source, and lie in one of the major *Herschel* fields, we could be selecting a population of lower redshift or warmer clusters/protoclusters than found by Planck Collaboration XXXIX (2016d).

Local galaxies and cirrus have mean 857/545 colours of 3.0 ± 1.0 and 2.8 ± 0.7 respectively, whereas the unassigned sources have a colour of 2.5 ± 1.0 . For the unassigned sources, nine of the 35 have colours that would have been selected in Planck Collaboration XXXIX (2016d) as potentially high redshift. It is therefore not unreasonable to suggest that unassigned sources with both red colours and a large, but not overdense, number of *Herschel* sources could also be high-redshift protoclusters of *Herschel* sources. Our lens candidates have a median 857/545 GHz colour of 1.8 ± 0.5 , and our QSO has 857/545 GHz colour of 0.8 ± 0.4 at a redshift of 2.099. The three stars have a mean 857/545 GHz colour of 3.0 ± 0.4 . As expected, the stars, local galaxies, and cirrus all have 857/545 colours that indicate that they are at redshifts $\ll 1$, whereas the red-

shift 2.099 QSO, lens candidates and our protocluster candidates have colours that indicate they lie at redshifts > 1 .

The total colour from a candidate protocluster will be a combination of foreground/background sources and sources associated with the protocluster. This is especially important, considering that overdensities of *Herschel* sources have been argued to be due to line-of-sight effects from multiple clusters, both theoretically (Negrello et al. 2016) and observationally (Flores-Cacho et al. 2016). In order to assess the contribution from foreground sources to the colour of a *Planck* source, we simulated the *Planck* colours of a region of sky containing a protocluster. Our simulated protoclusters have, on average, 11 members which would be selected by our flux cut-off, and we include contribution from sources not associated with the protocluster by adding in, on average, nine sources which would be selected by our flux cut-off randomly distributed between redshifts 1 and 3. The total number of detected sources in then around 20, which is just high enough to be selected as a candidate protocluster for our sample. For all sources, we drew samples from a single-temperature modified blackbody function

$$S_\nu \propto \nu^\beta B_\nu(T), \quad (2)$$

where ν^β modifies the emissivity function of the dust and $B_\nu(T)$ is the *Planck* function at temperature T . The temperature was fixed at 29 K and β was fixed at 2, so that the background sources have an average S_{857}/S_{545} flux density ratio that matches that seen in the *Herschel* maps, in this case $S_{857}/S_{545} = 1.87$. The fluxes of each source are drawn from an exponential distribution, which roughly matches the distribution of fluxes we see in our catalogues of 350 μ m detected *Herschel* sources, and our 350 μ m flux is then normalized to this value. We simulate four protoclusters in total, at redshifts 1, 2, 3, and 4, and for each redshift we draw 100 protoclusters using the method described above. We determined the total colour by summing the total 857 GHz flux density and dividing by the total 545 GHz flux density from all sources. The results of this are shown in Fig. 8.

We find that when there are few protocluster sources compared to background/foreground sources, the colours tend to the average colours of the foreground/background sources, as expected, and in this case with an average of $S_{857}/S_{545} = 1.87$. Once there are roughly equal number of protocluster sources and background/foreground sources however, the protocluster tends to dominate the colour of the source. However, that colour is dominated by the redshift of the source, with protoclusters at redshifts 3 and 4 having a lower S_{857}/S_{545} flux density ratio, protoclusters at redshift 1 having a higher S_{857}/S_{545} flux density ratio. If a protocluster is roughly at the same redshift as the average redshift of the background/foreground sources, then there is no obvious difference in its colour compared to a patch of sky where there is no protocluster. This provides a simple explanation for the ‘warm’ protocluster candidates that they are lower redshift clusters/protoclusters compared to the likely high- z clusters detected in the PHZ (Planck Collaboration XXXIX 2016d). However, we note in particular that our results are very sensitive to the assumption that all our galaxies are the same temperature; even if we allow the temperature to vary by ± 5 K, the standard deviation in the S_{857}/S_{545} flux density ratios of protoclusters can double from 0.1 to 0.2 for a protocluster at redshift 2. This further suggests that there can be significant boosting both into and out of the selection region used by the PHZ, though the general trend remains that higher redshift protoclusters tend to have lower S_{857}/S_{545} flux density ratios. The major benefit used in this paper compared to the PHZ is that we do not make any colour selection, and are therefore sensitive to clusters/protoclusters at all redshifts where we would detect them by our flux cut.

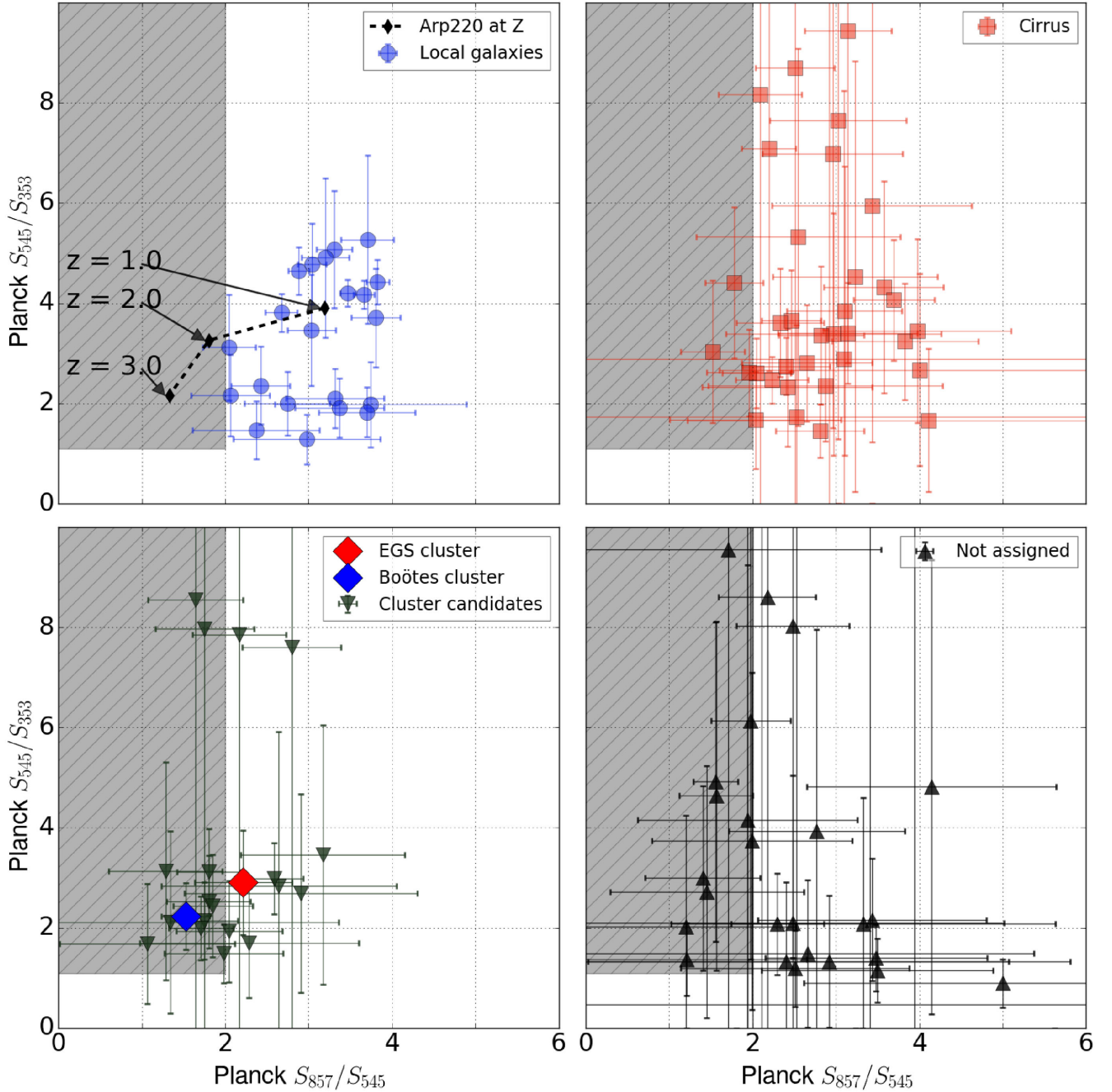


Figure 7. *Planck* 857/545 GHz and 545/353 GHz colours for the categories of source we identify as local galaxies (top left), cirrus sources (top right), cluster candidates (bottom left), and unassigned sources (bottom right). The grey-shaded region represents the selection criteria used in *Planck* Collaboration XXXIX (2016d) for their selection of high-redshift source candidates. The black line in the top left plot shows the *Planck* colours of Arp 220 as it would appear at $z = 1, 2$, and 3, and the blue and red diamonds in the protocluster candidates plot show, respectively, the BOOTES and EGS protocluster candidates identified in Clements et al. (2014).

5.2 *Herschel* colours

The use of *Herschel*–SPIRE colour-colour diagrams to separate sources of different redshifts is well established (e.g. Herranz et al. 2013; Noble et al. 2013; Clements et al. 2014; Ivison et al. 2016; Negrello et al. 2016), though the precise interpretation of the results are uncertain. Typically, sources whose Spectral Energy Distribution (SED) peak at longer wavelengths tend to lie at higher redshifts (Casey et al. 2014; Dowell et al. 2014; Asboth et al. 2016; Ivison

et al. 2016), and therefore sources whose SED peak at 250, 350, and 500 μm likely indicate progressively higher redshifts.

In Fig. 9, we simulate the *Herschel* colours, again using a single-temperature modified blackbody function, in an attempt to show the rough redshift a source is likely to have, given its *Herschel* colours. We fix the redshifts at 0, 2, and 4, where we expect our sources to approximately peak in the three SPIRE bands, and uniformly distribute the temperatures and β values between 20 and

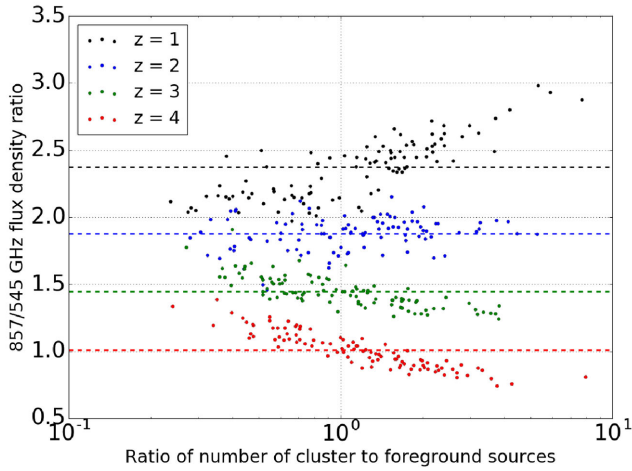


Figure 8. Estimated *Planck* 857/545 GHz flux density ratio of 400 protoclusters, as a ratio of the number of protocluster to background/foreground sources. Points in black are protoclusters at a redshift of one, in blue at a redshift of two, in green at a redshift of three, and in red at a redshift of four. The dashed lines show the average colour of the 100 protoclusters at each redshift. Large symbols show protoclusters which would be selected by our 3σ overdensity requirement, with small labels showing protoclusters that would not be.

60 K and 1 and 2.5, respectively. Fig. 9 shows that the *Herschel* colours of a source can provide a good proxy for the redshift of that source.

To compare to our simulation, in Fig. 10, we plot the individual S_{250}/S_{350} and S_{350}/S_{500} *Herschel* colours for the local galaxies and protocluster candidate *Planck* sources. Any local galaxy extended on arcminute scales, or where extraction on the *Herschel* map has clearly divided the source into multiple sources was removed. For the 250/350 and 350/500 μm colours of the local galaxies, we find a mean of 2.05 ± 0.43 and 2.60 ± 0.74 , respectively, whereas for the protocluster candidates these values are 1.13 ± 0.47 and 1.57 ± 0.49 . Fig. 10 clearly divides into two regions, one bluer region associated with the local galaxies, and one red region where the bulk of the *Herschel* detected protocluster candidates lie. Similar to the *Planck* colours, the *Herschel* colours of the protocluster candidates are on average redder than for the local galaxies. At the same time, we take a template starburst galaxy, Arp 220 (Donley

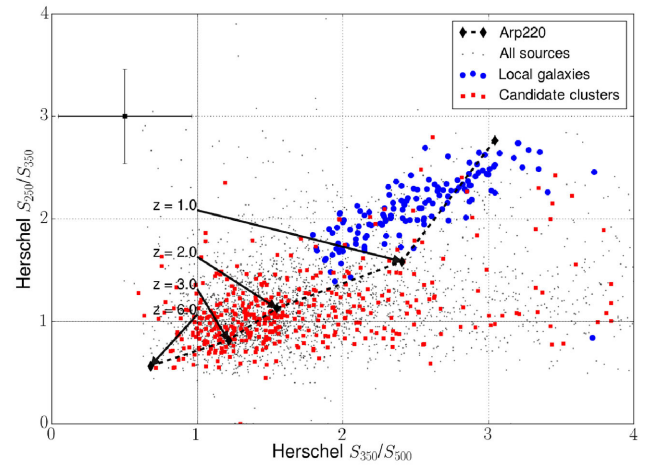


Figure 10. *Herschel* S_{250}/S_{350} and S_{350}/S_{500} colours of local galaxies (blue circles) or all the *Herschel* sources associated with the protocluster candidates (red squares). The small black circles include all *Herschel* sources detected for all of our *Planck* sources. Typical errors are given on the left (black square). The dashed black line with the black diamonds shows the *Herschel* colours of the local DSFG Arp 220, as it would appear at $z = 2, 4$, and 6.

et al. 2007), and examine the *Herschel* colours as it would appear at various redshifts. Direct comparison suggests the protocluster candidates lie at a redshift of $\simeq 2$. This is also in good agreement with our estimates of single-temperature blackbody fits in Fig. 9, with local galaxies inhabiting the low-redshift region and protocluster candidates inhabiting the region suggested for redshifts between 2 and 4. However, estimating the redshift of sources from its *Herschel* colours alone can be difficult; often the errors are large, and the variation seen in Figs 9 and 10 alone is enough to make the true redshift of a source uncertain. Given the simulations, observed error, and variation we see here, we can therefore reasonably say these sources likely lie at $z > 1$, but little more until future follow-up work can constrain these sources further.

6 THE CANDIDATE CLUSTERS

Out of the 279 unique *Planck* sources we have identified, 27 appear to be $>3\sigma$ overdensities of *Herschel* sources. The photometry of

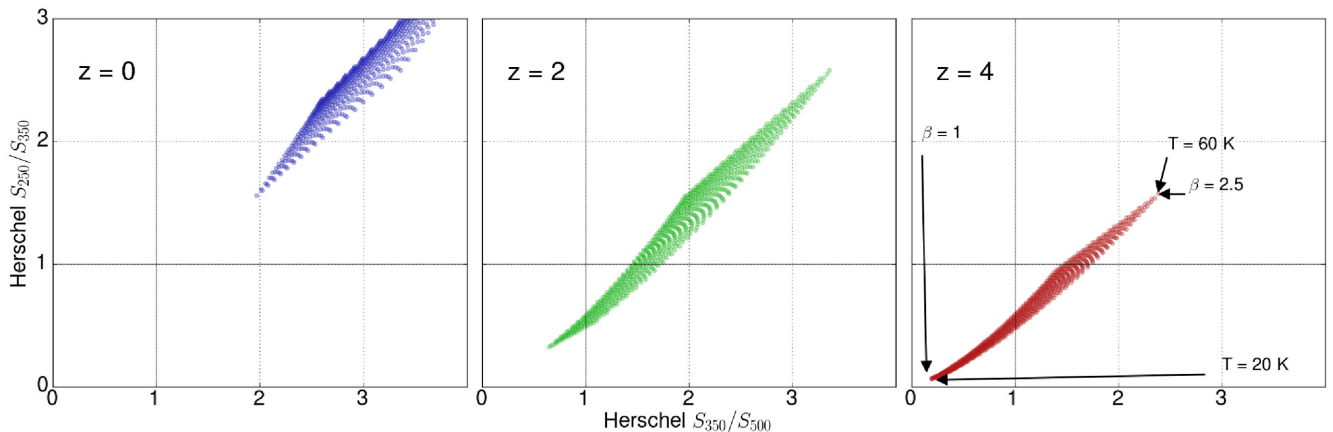


Figure 9. The *Herschel* S_{250}/S_{350} versus S_{350}/S_{500} colours for modified blackbodies (see the text for more detail) at redshifts of 0, 2, and 4, allowing T and β to vary between 20 and 60 K and 1 and 2.5, respectively. In the far right plot, the regions of maximum and minimum T and β are indicated for clarity.

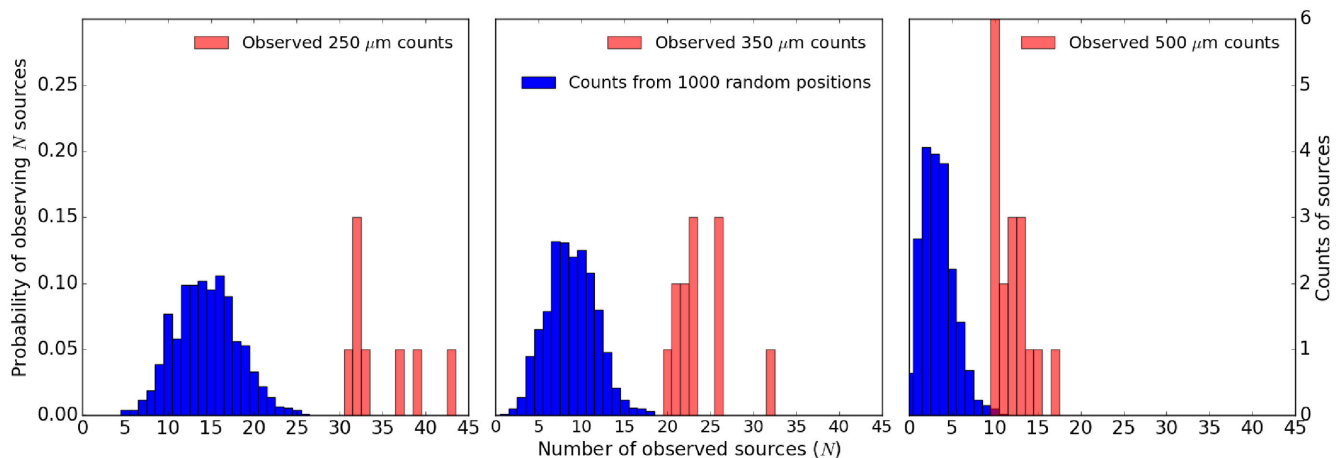


Figure 11. (Blue) Histograms of the result when 1000 random *Planck* beams are placed on the NGP map and the number of sources with S_{350} , S_{250} , or $S_{500} > 24.5$ mJy are counted for: (left) the 250 μm band, (middle) the 350 μm band, and (right) the 500 μm band. (Red) Histograms of the observed numbers of 250, 350, and 500 μm sources for our candidate protoclusters, which are considered overdense in their respective bands.

these objects indicates that the flux density comes from a number of discrete, individual sources, and their colours indicate that they likely lie at $z \sim 2$. These observations could correspond to a physical cluster of DSFGs, a series of line-of-sight sources stretching from $z \sim 2$ to ~ 4 , or multiple clusters/protoclusters along the line of sight. In this section, we attempt to quantify these protocluster candidates further, and examine whether the large area surveyed can explain these sources through fluctuations in the number counts alone.

6.1 Probability of observing $>N$ sources by chance

If our candidate protoclusters are actually only line of sight or number count fluctuations, then it should be possible to model the probability of finding one using Poisson statistics. In Fig. 11, we sample the NGP field with 1000 random *Planck* beams of radius 4.63 arcmin, and count the number of 250, 350, and 500 μm sources with fluxes greater than 25.4 mJy in each of the three respective bands. We then plot the normalized version of this sample, as well as histograms of the numbers of *Herschel* sources associated with each of our candidate protoclusters from the 857 GHz band. Our candidate protoclusters are clearly overdense with respect to our random samples of 1000 positions. The mean number of associated *Herschel* sources for our protocluster candidates is 29.1, 20.6, and 10.7 for the 250, 350, and 500 μm bands, respectively, corresponding to a 2.9σ , 3.5σ , and 4.0σ overdensity, respectively.⁵

Given we here examine roughly 800 deg^2 of sky, and according to Poisson statistics, we may expect to find around 76 patches where there are 29.1(30) or more 250 μm sources, 21 regions where there are 20.6 (21) or more 350 μm sources, and 1 region where there are 10.7 (11) or more 500 μm sources. If all our protoclusters were only this overdense, this might partially explain our results, however, many of our protoclusters host far stronger overdensities, with 14 of our protocluster candidates containing ≥ 36 , 23, or 12 250, 350, and 500 μm sources, respectively (with maximal numbers of associated *Herschel* sources of 43, 32, and 17 for the

three bands). Over 800 deg^2 of sky, we would therefore expect to see 0.5, 1.5, and 0.3 patches containing ≥ 36 , 23, or 12 250, 350, and 500 μm sources, if they were Poisson distributed. We in fact see four patches at least this overdense in the 250 μm band, eight at least this overdense in the 350 μm band, and 10 at least this overdense in the 500 μm band, which cannot be explained solely by the large area surveyed in this paper. Our candidate protoclusters are therefore likely to be physically associated or be the product of several clusters/protoclusters or overdensities along the line of sight.

We would still expect some level of contamination from unassociated sources. Under the assumption that the *Herschel* sources are a mix of protocluster members and Poisson distributed unassociated sources, for an expected μ sources, the probability that there are N protocluster sources out of M detected sources is given by:

$$p(N|M, \mu) = \frac{\left[\frac{\mu^{(M-N)}}{(M-N)!} \right]}{\sum_{i=0}^{i=M} \left[\frac{\mu^{(i)}}{(i)!} \right]}, \quad (3)$$

the derivation of which is given in Appendix C. For our mean of 20.6 350 μm *Herschel* sources associated with each cluster, this suggests that on average, around 11 of the sources would be associated with the protocluster, with only a 0.7 per cent chance of having three or fewer protocluster members.

Though we do not have accurate redshifts for our sources, we can get some idea if they lie at similar redshifts by examining where the individual *Herschel* sources for a single protocluster candidate lie in colour-colour space. In Fig. 12, we plot the *Herschel* colours for the *Herschel* components of three of our *Planck* sources; the BOOTES protocluster identified by Clements et al. (2014), a candidate protocluster PCCS1 857 G085.48+43.36 identified in this work, and a cirrus source. The BOOTES protocluster and the ELAIS-N1 protocluster show clear clustering in the colour-colour plot, whereas the cirrus source shows a much larger spread. From Fig. 9, this clustering in colour-colour space indicates that it is likely these sources are physically associated, but the uncertainties are large enough that we cannot rule out the possibility that these multiple clusters/protoclusters along the line of sight.

⁵ These probabilities have been converted to their corresponding σ value in the normal distribution.

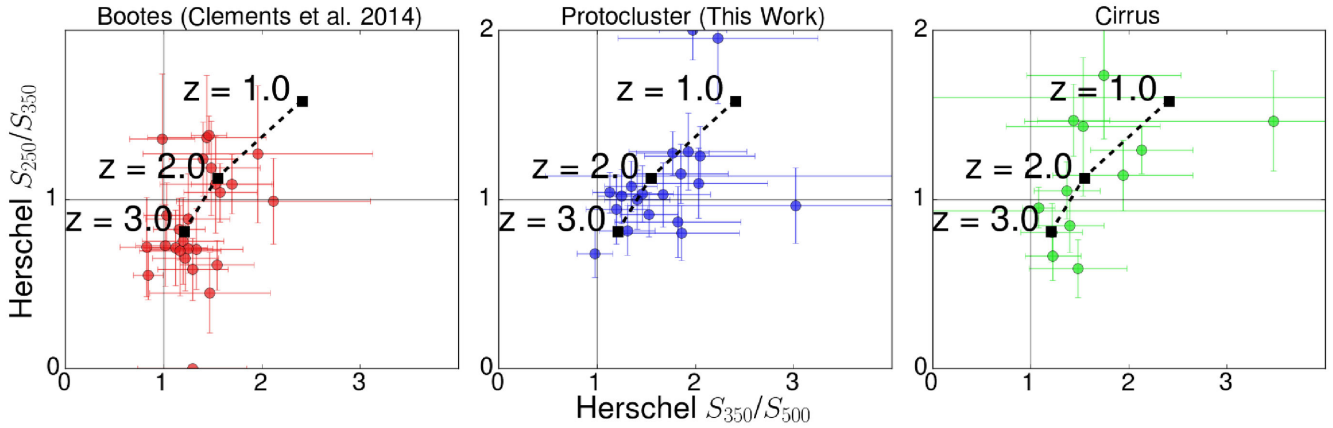


Figure 12. *Herschel* S_{350}/S_{500} S_{250}/S_{350} plot showing the colours for three *Planck* sources; the BOOTES clump identified by Clements et al. (2014) on the left; a candidate cluster seen in the ELAIS-N1 field in the centre, and a source identified with Galactic cirrus on the right. The black dashed line and squares indicate the *Herschel* S_{350}/S_{500} and S_{250}/S_{350} of the local DSFG Arp 220, as it would appear at $z = 1.0$, 2.0 , and 3.0 .

6.2 Properties of the protocluster candidates

Given our previous analysis, in the following sections, we assume that all 27 of our candidate protoclusters are physically associated protoclusters or multiple clusters/protoclusters along the line of sight, as opposed to chance overdensities along the line of sight. We find a surface density of candidate protoclusters of $(3.3 \pm 0.7) \times 10^{-2}$ protoclusters deg^{-2} . In their assessment of the number of *Planck* detectable clusters, Clements et al. (2014) find a surface density of $(4.4 \pm 2.2) \times 10^{-2}$ sources deg^{-2} , in good agreement with our results here. *Planck* Collaboration XXXIX (2016d) in the PHZ, searched directly on the *Planck* maps, discovering a total of 2151 candidate high- z sources across around $10\,000 \text{ deg}^2$ of the cleanest part of the sky, with initial follow-up suggesting 94 per cent of these are overdensities of sources (*Planck* Collaboration XXVII 2015). Given the different selection functions used in the PHZ and this paper, it is difficult to make a direct comparison, but this would correspond to an approximate surface density of (0.18 ± 0.01) sources deg^{-2} , roughly five times larger than found here. This can be somewhat offset if we include our sources where do not assign a classification, as our surface density rises to (0.11 ± 0.02) sources deg^{-2} , in closer agreement with the PHZ. Further follow-up of the PHZ sources, especially at the fainter end, is needed to investigate the discrepancies.

The number counts within individual fields mostly agree with the estimated number counts given here, with 10 out of an expected 11 from the SGP, seven out of an expected six for the NGP, zero out of four for HerS (which has large amounts of Galactic cirrus), and roughly one in each of the smaller HerMES fields. The GAMA fields are lacking in sources, with no protocluster candidates detected in any of them. The lack of objects in GAMA could be due to the large amount of foreground cirrus present in GAMA09 and GAMA15, which could obscure a number of candidate protoclusters.

Many confirmed protoclusters are found to be extended on scales of tens of arcminutes (Casey 2016). The smaller *Planck* beam implies that we are detecting highly compact systems of DSFGs, compared to generic protoclusters which tend to show less of a density contrast with respect to the background (Casey 2016). For instance, the BOOTES protocluster candidate appears to be at a redshift of $z \sim 2.3$. Pearson et al. (2013) estimate the redshift distribution of sources in the phase 1 release of H-ATLAS, where they find there should be roughly 10–100 *Herschel* sources per square degree with $F_{350} > 35 \text{ mJy}$ at a redshift ~ 2 , or roughly 0.2–1.5 sources per

Planck beam. Using the definition of Chiang, Overzier & Gebhardt (2013) of density contrast:

$$\delta_{\text{gal}}(\mathbf{x}) = \frac{n_{\text{gal}}(\mathbf{x}) - \langle n_{\text{gal}} \rangle}{\langle n_{\text{gal}} \rangle} \quad (4)$$

and a simple photo- z fitter, which fits our *Herschel* sources to a SED template of Arp 220, we find 12 sources with $F_{350} > 35$ whose photo- z is consistent within 1σ of $z = 2.3$, giving a density contrast between $\delta(12) = 7$ –60, depending on whether one uses a low or high estimate of the density of *Herschel* sources at $z = 2.3$. The low-density contrast estimate is still consistent with these sources being protoclusters, but for density contrasts of > 10 this becomes more difficult to understand; the large density contrasts imply that these are systems which are well on their way to collapse and virialization. However, two of our candidate protoclusters appear to be associated with known galaxy clusters; PCCS1 545 G058.72+82.59 (PCCS1 857 G058.53+82.57) lies 4.3 arcmin away from the core of galaxy cluster GHO 1319+3023 (Gunn, Hoesel & Oke 1986) at a redshift of 0.4, PCCS1 545 G027.38+84.85 (PLCKERC857 G027.36+84.83) is associated with the redshift 0.43 galaxy cluster GMBG J198.59994+26.5688 (Hao et al. 2010) and PCCS1 545 G084.40+81.05 is associated with the estimated redshift 0.43 galaxy cluster NSCS J131812+335831 (Lopes et al. 2004). Given our earlier estimates on the redshift of our sources being at $z > 1$, it is possible that our cluster of DSFGs is being lensed by a foreground cluster, rather than that they are physically associated with the foreground cluster. Three of our protoclusters, PLCKERC857 G017.86–68.67, PLCKERC857 G149.81+50.11, and PLCKERC857 G095.44+58.94, also appear to host QSOs that are mostly, not emitting in the FIR. Again, whether or not these QSOs are associated with the cluster of DSFGs is uncertain, but these redshifts are typically between $z = 1$ and 2 , so could be signposting the true redshifts of our protoclusters.

6.3 Simulations of DSFGs in clusters

Granato et al. (2015) simulate the FIR/sub-mm properties of high-redshift clusters and protoclusters by combining hydrodynamical simulations with GRASIL-3D, a radiative transfer code that accounts for dust reprocessing in arbitrary geometries. In Fig. 13, we compare the number counts of clusters of DSFGs from the *Herschel* data with the predicted number counts obtained by Granato et al. (2015),

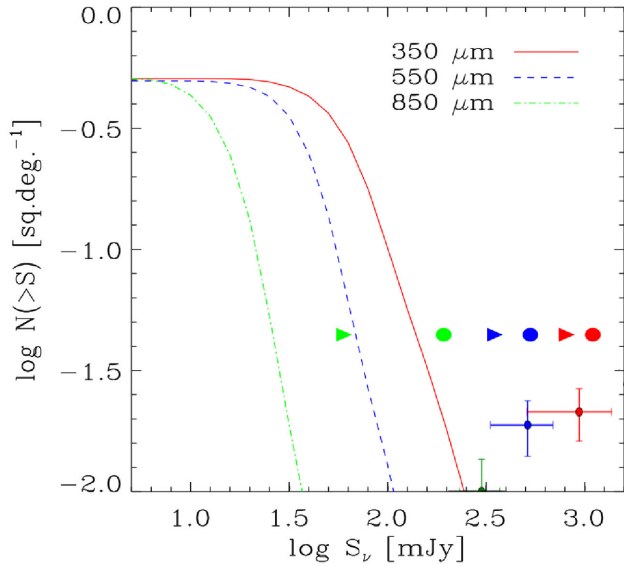


Figure 13. Expected cumulative number counts of clusters reproduced from Granato et al. (2015). The solid, dashed, and dot-dashed lines show the predicted number counts of sources at 850, 550, and 350 μm . The circles and right pointing triangles are the results from Clements et al. (2014), and points with error bars are the results from this work.

assuming their 24 simulated clusters, which all had a final virial mass at $z = 0$ above $1 \times 10^{15} h^{-1} M_{\odot}$, are representative of the cluster population we detect here. We impose a 3σ S/N cut for each band considered, and use the aperture photometry estimate from *Planck*. Again, we assume that all our 27 candidate protoclusters are actual physical clusters of sources. Our observations indicate that our detected clumps are more numerous, or are brighter, than predicted from these simulations. The flux density from our protoclusters appear to be on average ~ 5 times greater than predicted.

In Fig. 14, we show that this is likely due to our observed sources being brighter than expected in simulations, by reproducing the histogram of expected 350, 550, and 850 μm flux densities from Granato et al. (2015), and comparing the distribution of the 350 μm flux densities of the protoclusters identified in this work. Since some of the flux from our protocluster candidates will come from sources not associated with the protocluster, we attempt to remove this foreground contribution. We place 1000 *Planck* beams at random positions on each of the *Herschel* maps, calculate the total flux density in those beams following the same prescription in Section 4, and take the median value of the aperture fluxes over those 1000 beams as the typical foreground contamination. The median value varies between maps, but is usually of the order of 100–300 mJy.

These values are then removed from the *Herschel* aperture flux densities for each of the protoclusters, and the results plotted in Fig. 14. The difference between our observed flux densities and the simulated clusters is exacerbated at higher redshifts, as the simulated flux densities tend to decrease (Granato et al. 2015). The original plots in Granato et al. (2015) split the data into three separate redshift bins at $z = 1, 2$, and 3, with the $z = 1$ flux densities generally being the greatest. Therefore, to be conservative, we compare our results to those at redshift $z = 1$, under the extreme assumption that all our candidate protoclusters exist at this redshift. Even in the extreme case that all our candidate protoclusters lie at $z \simeq 1$, the observed flux densities appear systematically higher than the simulated flux

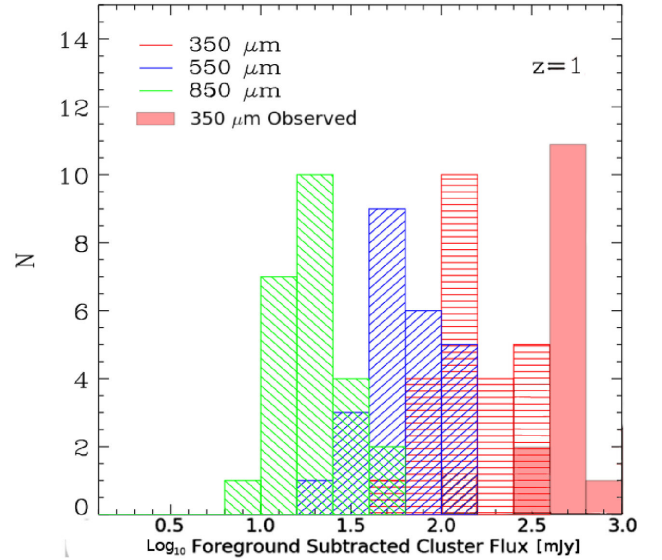


Figure 14. A histogram of the estimated flux densities of clusters at $z = 1$ reproduced from Granato et al. (2015). The red, green, and blue hashed bins represent the histograms from the simulation of clusters as they would appear in the *Planck* HFI bands. The solid red histogram gives the foreground subtracted candidate protocluster flux densities from this work if placed at $z = 1$.

densities, with a median flux density of protocluster candidates of 500 mJy at 350 μm observed compared to 100 mJy simulated.

It is difficult to match the observed protocluster flux densities to the simulated. We earlier demonstrated that the flux from these sources comes almost entirely from multiple, detected, discrete sources rather than cirrus or fainter sources. Additionally, we remove any foreground or background contaminant and compare our sources to those simulated clusters with the highest flux densities. Even with these constraints, we still find our protoclusters are around a factor of 5 times brighter in comparison to the simulations. If these protoclusters are confirmed to be real, physical associations, then these results demonstrate that current models of cluster formation struggle to reproduce the FIR/sub-mm flux densities seen in observations by a factor of 5, and likely underestimate the star formation rate (SFR) in clusters/protoclusters during their formation. One possible explanation is that these DSFGs are not tracing only the most massive clusters, and that clusters with lower final virial masses could match our observations, but redshift and mass confirmations would be required before this can be tested.

6.4 Evolution of large-scale structure

According to the formalism of Negrello et al. (2005), the number counts of clusters should be sensitive to the evolution of the amplitude Q of the three-point correlation function. Under the tentative assumption that the galaxies in our protocluster candidates are in fact all physically associated, we compare the counts of our candidate protoclusters to the predictions made by Negrello et al. (2005) in Fig. 15. We plot both our result when no restrictions are imposed (in blue) and when we impose the constraint that only the seven protocluster candidates detected to at least 3σ in the 353 GHz channel (850 μm) are included (in green). Without constraints, we find a median flux for our protoclusters of (169 ± 95) mJy, and a number density of 135 ± 24 sources per steradian. With constraints, we find

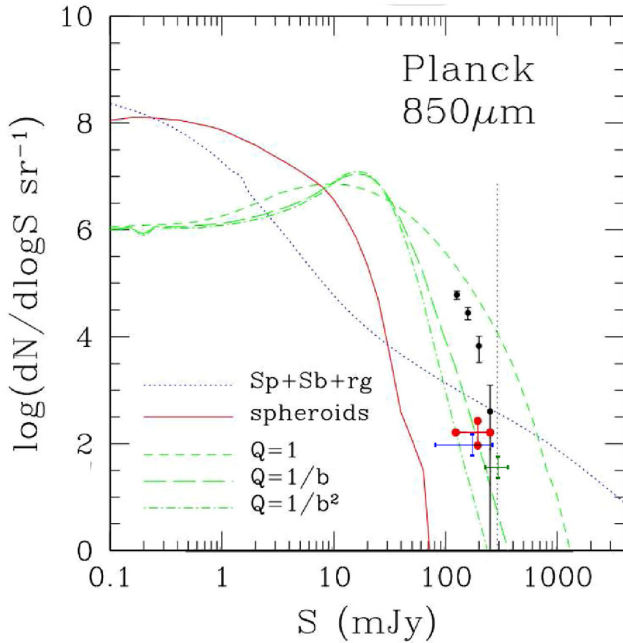


Figure 15. Predicted number counts for overdensities of 850 μm sources taken from Negrello et al. (2005). The dashed green lines give the predictions for the number counts as the three point correlation function evolves according to $Q = 1$ (no evolution) $Q = \frac{1}{b}$ and $Q = \frac{1}{b^2}$, where b is the linear bias factor between galaxies and dark matter. The black points are from the simulations from Negrello et al. (2005), the red point gives the results from Clements et al. (2014), and the blue point gives the results from this paper using all our protoclusters. The green point is our result if we restrict ourselves only to protoclusters detected at the $>3\sigma$ level.

a median flux for our protoclusters of (294 ± 65) mJy, and a number density of 39.4 ± 13 sources per steradian.

Both Clements et al. (2014) and this work strongly exclude the $Q = 1$ analytical model, which corresponds to the amplitude Q of the three-point correlation not evolving with redshift. Using 3σ detected protoclusters at 353 GHz suggests that the $Q \propto \frac{1}{b^2}$ model is also incorrect. However, caution should be taken as these are only candidate protoclusters rather than confirmed, and with only seven protoclusters detected to 3σ the number counts remain low. Additionally, flux contamination from unassociated sources (which we account for in Section 6.3 but cannot account for here) is likely to play a role. If we assume that roughly 25 per cent of the flux can be from unassociated sources, similar to what was found in Section 6.3, our conclusions remain similar, with a better agreement between the $Q = \frac{1}{b}$ model and our $>3\sigma$ detected protoclusters.

7 DISCUSSION

We have identified 27 candidate protoclusters from a cross-match of *Planck* compact source catalogues and *Herschel* maps. The numbers of sources are difficult to explain if none of them are associated with each other, and their colours indicate they all likely lie at $z > 1$. We have also found several protocluster candidates with lower S_{857}/S_{545} flux ratios than expected. We have shown this could be from a large number of foreground contaminants, but it is also possible that there exists a warmer population of clusters/protoclusters of DSFGs. In this section, we discuss these results in the context of the literature, as well as briefly discussing the natures of the other *Planck* compact sources we have identified.

7.1 The HeLMS field

The HeLMS (PI: Marco Viero) is a shallow 280 deg² field imaged with *Herschel*–SPIRE at 250, 350, and 500 μm . In comparison to the other extragalactic fields under consideration here, it is highly contaminated by cirrus. No publicly released, verified catalogue exists for this complex field, but using a private catalogue (Viero, private communication), we find 130 857 GHz and 40 545 GHz *Planck* compact sources in this field, and 137 unique sources. The maps are highly cirrus contaminated, with 64 (46 per cent) of sources being identified with Galactic cirrus, 61 (45 per cent) local galaxies, 2 QSOs (LBQS 0106+0119 and CRATES J2323–0316), 1 candidate protocluster, and 9 sources with no clear identification. Even in the PCCS2, where we found that only 2.5 per cent of sources were associated with Galactic cirrus, we find 27 per cent of PCCS2 sources in the HeLMS field are associated with Galactic cirrus.

Overall, given the reasonably small differences found between the other H-ATLAS, HerMES, and HerS fields, and the large differences found between them and HeLMS, we ascribe the differences in our results to the complex nature of the HeLMS field, and the preliminary nature of the catalogues currently available.

7.2 The nature of the *Planck* compact sources

Figs 3 and 4, and Table 2 all indicate that the *Planck* compact sources resolve into a range of different phenomena. Furthermore, almost half of the *Planck* compact sources are actually extended on the scale of *Herschel*, so filters designed purely for point-like sources can miss a range of sources, as shown in Table 3. Given this, the ERCSC, PCCS, and PCCS2 should not simply be considered deeper versions of the same catalogue, but catalogues that specifically probe different source types owing to the different filters and extraction methods used in their creation.

The *Planck* compact source catalogues appear to host several stars. Two of the three stars present in our catalogue, Mira (also known as o Ceti), and R Sculptoris, are both asymptotic giant branch stars, known to produce large amounts of dust (Mayer et al. 2011; Maercker et al. 2016), whilst the third, α PsA o, is known to host a dusty debris disc (Acke et al. 2012).

One of our lens candidates, like our protocluster candidates, appear to host an overdensity of *Herschel* sources. These could indicate the presence of a physical cluster or protocluster. PLCK-ERC857 G047.32+82.53 (H-ATLAS J132426.9+284452, Negrello et al. 2016) at a redshift of 1.676 (George et al. 2013; Busmann et al. 2013; Timmons et al. 2015) has a 3.1σ overdensity of 500 μm sources. We also note that PCCS2 857 G270.56+58.54 (H12-00, Herranz et al. 2013; Fu et al. 2012; Clements et al. 2016) hosts 2.8σ overdensity of 350 μm sources and Clements et al. (2016) find an overdensity of SCUBA-2 850 μm sources associated with H12-00, and is unclassified in this work, though it is selected as a candidate protocluster if we use a slightly smaller beam size of 4.33 arcmin. Furthermore, H12-00 is also independently selected in Canameras et al. (2015), where they specifically search for and follow-up the brightest gravitational lensed sources discovered with *Planck*. Whether DSFGs are good tracers of the most massive dark matter overdensities at $z > 2$ continues to be widely debated (Blain et al. 2004; Chapman et al. 2009; Dannerbauer et al. 2014; Miller et al. 2015; Casey et al. 2015; Hung et al. 2016), but if they do, then these lensed sources could make excellent signposts for the locations of further clusters/protoclusters.

H12-00 (Clements et al. 2016) does not qualify as a protocluster candidate using our criterion in Section 3. Given that follow-up

work on H12-00 demonstrates its likely cluster nature (Clements et al. 2016), the large number of ‘red’ unassigned sources, and a number of sources that are on the edge of being selected as candidate protoclusters, it is entirely possible that *Planck* is detecting a far larger number of protocluster sources, but that the specific quantifiable criteria used here mean that they are not assigned as such during the selection process. An examination of the unassigned sources reveals almost half (28 of 61) have a $>2\sigma$ in the 250, 350, or 500 μm bands, but are not 3σ overdense. Additionally, three of the four matches we found with the PHZ were unclassified. So a closer examination of the archive (Both Harrington et al. 2016 and Geach et al. 2015) suggest this is a lensed $z = 2.553$ galaxy. Also known as SDSS J020941.27+001558.5. It is possible that several of the ‘red’ unassigned sources could be due to Cosmic Infrared Background fluctuations which, due to clustering, have a strong super-Gaussian tail so can appear as high S/N sources (See fig. 10 of De Zotti et al. 2015). However, Fig. 6 shows that the flux density of many of the unassigned sources is entirely accounted for by discrete, detected sources. These could still be line-of-sight chance alignments, but it does show that these are unlikely to be fluctuations in the background sources too faint to be detected by *Herschel* and are, at best, fluctuations in the number counts of bright ($S_{350} > 25.4 \text{ mJy}$) *Herschel* sources.

7.3 The nature of our protocluster candidates

DSFGs have now been found in a range of cluster environments, from extremely large protoclusters on angular scales >10 arcmin (Dannerbauer et al. 2014; Casey et al. 2015; Casey 2016), to scales similar to those of the *Planck* HFI beam (Herranz et al. 2013; Clements et al. 2014; Planck Collaboration XXVII 2015; Planck Collaboration XXXIX 2016d, this work), to >10 sources on ~ 20 arcsec scales (Oteo et al. 2017a). The existence of many physically associated DSFGs is surprising; simulations expect these sources to be physically unassociated (Hayward et al. 2013; Cowley et al. 2014), and without a mechanism for triggering several DSFGs simultaneously or a longer duty cycle (Emonts et al. 2016; Dannerbauer et al. 2017; Oteo et al. 2017b), we would not expect to observe several physically associated DSFGs at once (Casey 2016). Similar to the PHZ, we can be confident but not certain that the compact candidate protoclusters we have detected are physically associated or multiple clusters. However follow-up of other apparent overdensities of DSFGs (Flores-Cacho et al. 2016; Wang et al. 2016; Oteo et al. 2017a) suggests many of these objects are indeed physically associated. We leave redshift estimates and therefore SFR estimates for our protoclusters to a future paper (Cheng et al., in preparation), but if the DSFG members of these protocluster candidates are similar to other DSFGs, their likely SFR will be of the order of $100 \text{ M}_{\odot} \text{ yr}^{-1}$, and a likely total cluster SFR of up to several thousands of $\text{M}_{\odot} \text{ yr}^{-1}$ (Dannerbauer et al. 2014; Casey 2016; Oteo et al. 2017a). Both Scoville et al. (2013) and Darvish et al. (2016) find that below $z \sim 1$, SFR is efficiently quenched in denser environments, but the mechanisms for this quenching remain uncertain, and fig. 2 of Casey (2016) shows that there is clearly a downturn below $z \sim 1$ between the theoretical and observed SFR density of clusters. In this paper, we have found DSFGs, with elevated associated SFRs, in clusters/protoclusters over a range of scales, from the arcsecond to the arcminute. This indicates that it is unlikely that it is simply the scale or size of the structure that determines its SFR density. Given we do not see DSFGs in local clusters, it could be that it is the virialization state or the presence of a evolved intracluster medium which determines whether the presence of multiple DS-

FGs is likely to occur. No clusters containing significant numbers of DSFGs have so far been confirmed to be virialized, though the Spiderweb Galaxy structure may contain DSFGs in a virialized subhalo (Dannerbauer et al. 2014). If it is the virialization or presence of an evolved intracluster medium that prevents or quenches DSFGs, it would suggest that none of the protocluster candidates detected here, and indeed none of the confirmed clusters containing significant numbers of DSFGs, are yet virialized or possess an evolved intracluster medium. Finding clusters/protoclusters of DSFGs, and determining particularly the virialization and environmental state around and within them, may therefore be key to understanding the mechanisms behind the quenching of galaxies in different environments.

However, it should be stressed that the candidate protoclusters detected in this work remain candidates, and not only there is a need to confirm that the DSFGs detected lie at the same redshift, but further work should be undertaken to confirm that there is also an optical/NIR overdensity at these positions, confirming that this is indeed a cluster rather than associated sources that come from looking down a filament. Additionally, work should be done to characterize these clusters, particularly at what evolutionary stage they are at (i.e. have they virialized?). Both the PHZ and this work provide complementary targets for these systems on scales around a few arcminutes, with the PHZ generally selecting the brightest and reddest, and this work selecting both fainter and warmer candidates. Additional sources of cluster/protocluster candidates can come from selection directly on the *Herschel* maps (Valtchanov et al. 2013).

The diversity of DSFGs in clusters is further suggested by the difference we find with the PHZ; we only find four sources in common, none of which we identify as a candidate cluster. When applying their flux and colour cuts directly on our catalogue, we only find 15 objects, three (20 per cent) are cluster candidates [including the BOOTES cluster candidates identified by Clements et al. (2014)], three (20 per cent) are cirrus, four (26 per cent) are local galaxies (UGC 09215, UGC 08017, NGC 5056, and CGCG 160-170), one (6.6 per cent) is a lens candidate (H-ATLAS J132426.9+284452), and four (26 per cent), we were not able to assign an identity. Of these 15, 11 are detected only in the ERCSC.

Similar work has also been undertaken by Baes et al. (2014) in the 84 deg^2 of the *Herschel* Virgo Cluster Survey, where they find that most *Planck* compact sources are dominated by local late-type galaxies, with few sources being classified as Galactic cirrus, spurious detections, and no sources classified as candidate clusters. This can largely be explained by the small areas examined; As Baes et al. noted, they are directly examining a local cluster, whereas our total area surveyed is $\sim 10\times$ larger across most of the accessible extragalactic sky. Given also that they use the PCCS, which both they and we note is devoid of sources without a bright local counterpart (see Table 3), we therefore conclude that sky variance and use of PCCS1 can explain the apparently low numbers of cluster candidates in the *Herschel* Virgo Cluster Survey.

8 CONCLUSIONS

Through a cross-match of the *Planck* compact source catalogues, and 808.4 deg^2 of *Herschel* fields from H-ATLAS, HerMES, and HerS, we have identified 27 protoclusters of DSFGs that are at least 3σ overdense in either 250, 350, or 500 μm sources. Additionally, we have identified, 192 local galaxies, 43 regions of Galactic cirrus, 12 candidate lensed sources, three stars, and two QSOs which also make up the *Planck* compact source catalogues. A further 61 sources we are unable to assign a classification, but many host a large number

of *Herschel* sources ($>2\sigma$ in the 250, 350, or 500 μm bands), and other have colours indicative of a high-redshift origin. It is possible that many of these unassigned sources are also protoclusters of DSFGs, though it is more difficult to rule out fluctuations in the number counts as an explanation.

We find there is significant differences between the three released versions of the catalogues, with the ERCSC hosting a larger fraction of candidate protoclusters than the PCCS or PCCS2. We ascribe this to the filters used in the creation of the three catalogues, with the PCCS and PCCS2 Mexican-hat wavelet filter likely suppressing extended emission from both Galactic cirrus and candidate protoclusters.

We verified that there is good agreement between *Planck* and *Herschel* aperture photometries for all sources, and further find that with the exception of Galactic cirrus, simply summing up the detected *Herschel* source with S_{350} or $S_{500} > 25.4$ mJy results in a good match between *Planck* and *Herschel* photometries.

The *Planck* colours of our protocluster candidates indicate that a selection criteria of $S_{857}/S_{545} < 2$ performs well for selecting out candidate protoclusters. However, we have also found a number of warmer protocluster candidates, which would be missed by such a selection, though we have shown this can also be explained by a significant contamination of low redshift $z < 1$ DSFGs. The *Herschel* colours of our sources indicate they all likely lie at $z > 2$, and the small scatter of points in the *Herschel* colour–colour plots can indicate a physical cluster/protocluster, though the uncertainties are large.

We find a surface density of candidate protoclusters of $(3.3 \pm 0.7) \times 10^{-2}$ sources deg^{-2} , in good agreement with previous similar studies. Cross-matching our catalogue with the PHZ, we find only four matches, none of which we identify as a candidate protocluster.

Finally, we compare our results to simulations, finding both that our protoclusters are a factor of 5 times brighter at 353 GHz than expected from simulations, even in the most conservative estimates, and that the amplitude of the three-point correlation function Q likely evolves with $Q \propto \frac{1}{b}$.

Without redshift confirmation, there remains the possibility that none of these objects are physical clusters/protoclusters. However, given the number we have found alongside other groups, if they are clusters/protoclusters it is a challenge to explain how groups of >20 associated DSFGs exist, given their expected lifetimes of ~ 100 Myr. Such protoclusters of DSFGs are being found from arcminute to arcsecond scales, yet we do not see this in the local Universe, indicating that star formation is quenched in clusters at low redshifts, but does take place in clusters/protoclusters at higher redshifts, possibly due to cluster’s virialization state. Since we do not know if these sources are virialized, further characterization, particularly of the environment and state of virialization, should be a key focus for follow-up observations. Given also that we expect DSFGs such as these to evolve into the brightest cluster members at the cores of galaxy clusters, they likely play a vital role in the earliest stages of cluster formation and evolution.

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SUPPORTING INFORMATION

Supplementary data are available at [MNRAS](https://www.mnras.org) online.

Table B1. Candidate protoclusters from the *Planck* 857 GHz catalogues of compact sources. The σ values provide the strength of the overdensity at 250, 350, and 500 μm .

Table B2. Candidate protoclusters from the *Planck* 545 GHz catalogues of compact sources.

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APPENDIX A: IMAGES OF THE *Planck* COMPACT SOURCES

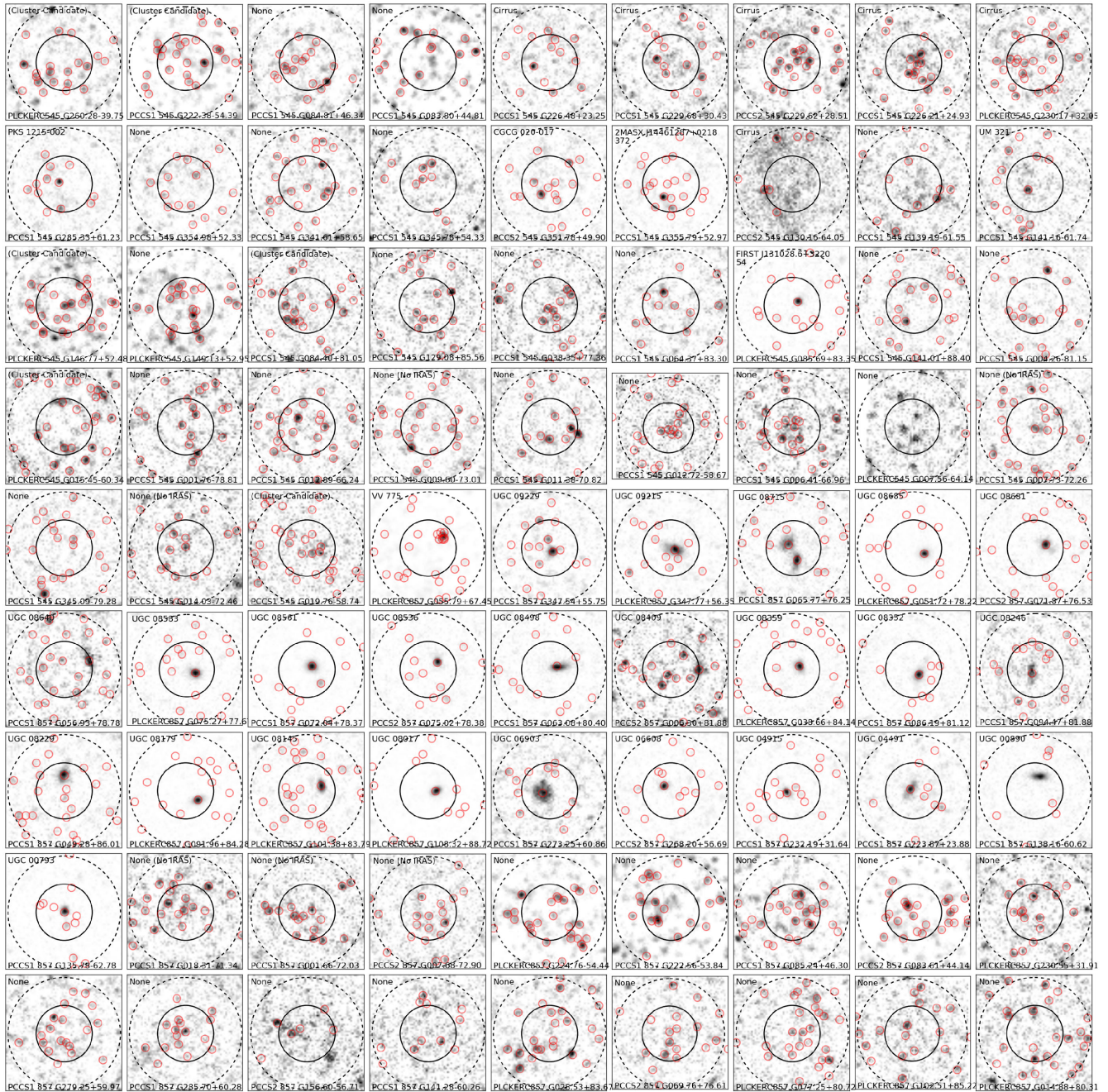


Figure A1. The 350 μm *Herschel* map for all of our sources, with the *Planck* beam in solid black circle, the aperture photometry in dashed black circle, and the red circles indicate the positions of sources which have a flux density >25.4 mJy in either the 250, 350, or 500 μm bands.

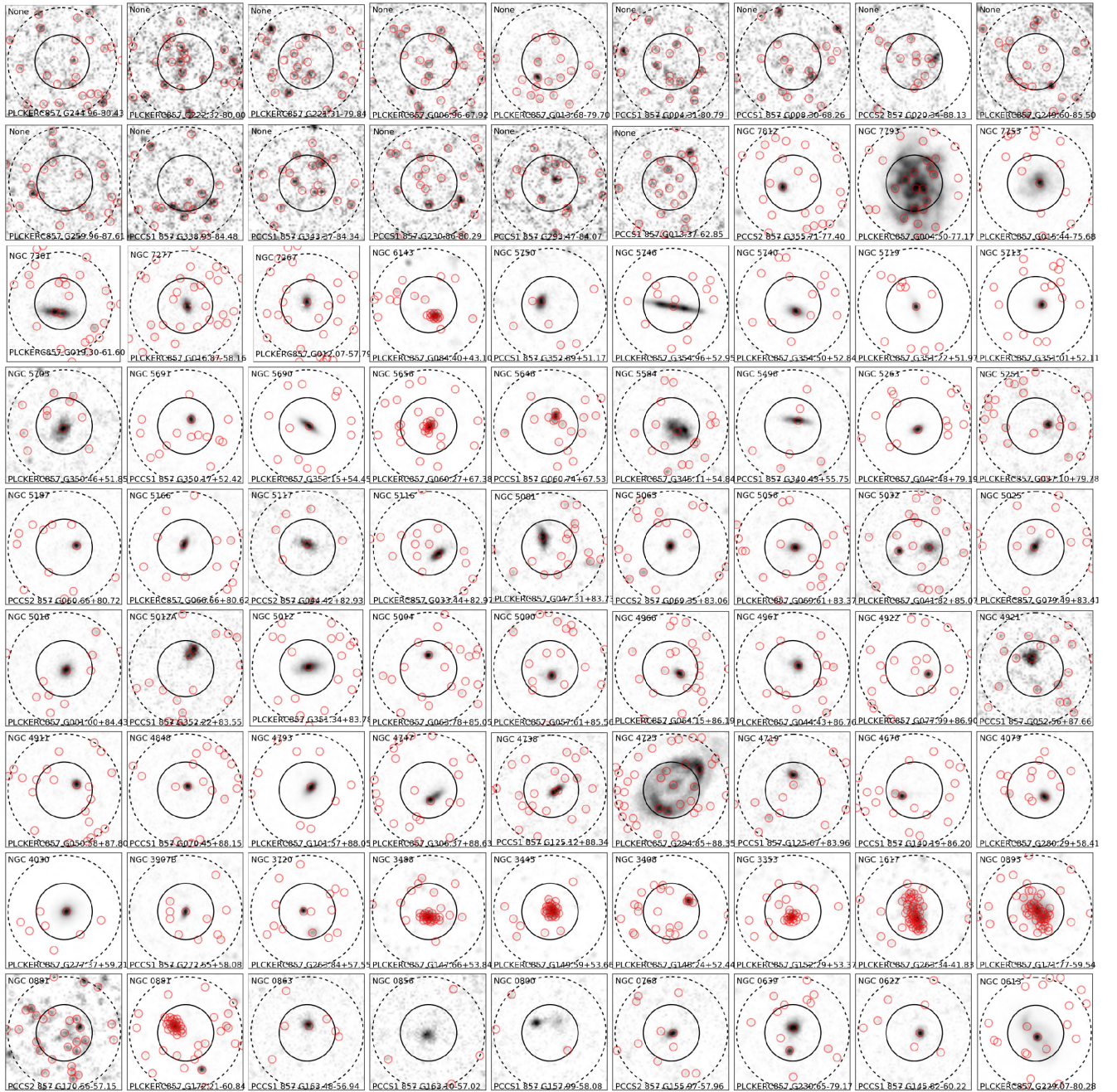


Figure A1 – continued.

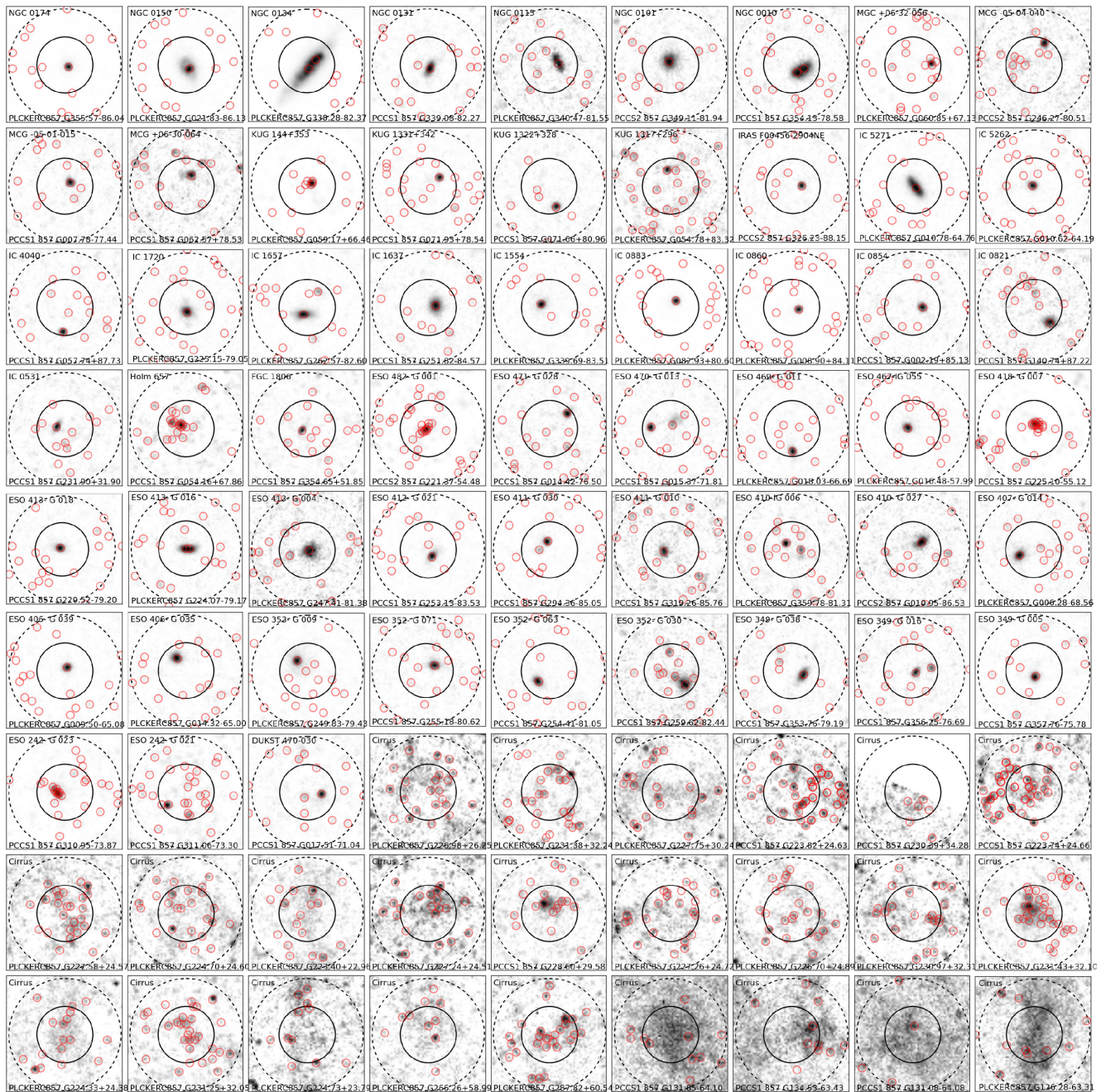


Figure A1 – *continued.*

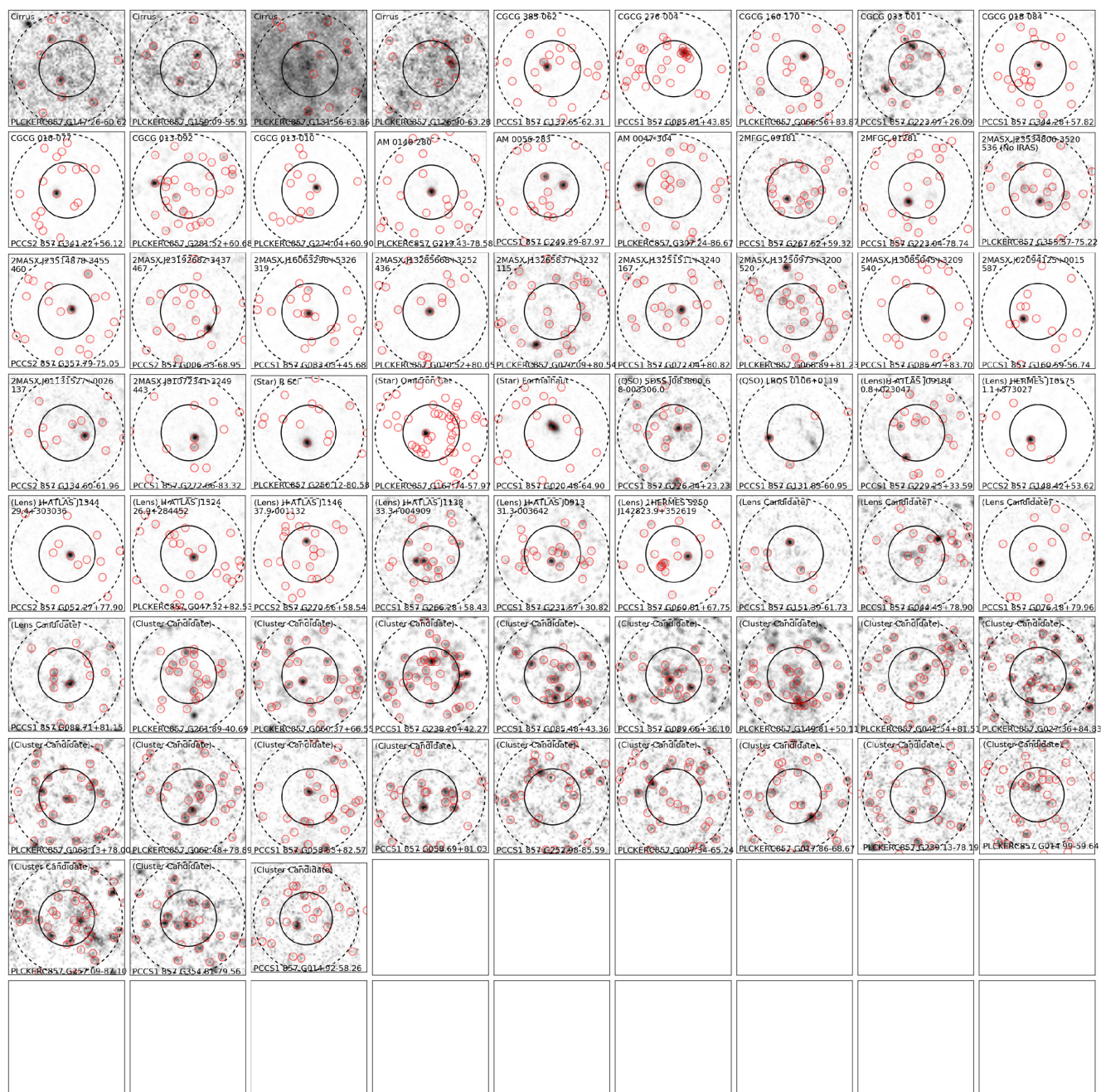


Figure A1 – *continued.*

APPENDIX B: TABLE OF THE *Planck* COMPACT SOURCES

Here, we include a list of all our *Planck* compact sources that lie on the maps.

Table B1. Candidate protoclusters from the *Planck* 857 GHz catalogues of compact sources. The σ values provide the strength of the overdensity at 250, 350, and 500 μm . A table containing the properties and identifications of all the *Planck* compact sources is available online.

Name	RA	Dec.	Associations	<i>Planck</i> 857 flux (mJy)	σ_{250}	σ_{350}	σ_{500}
PCCS1 857 G014.92–58.26	336.635	–32.177	Cluster candidate	302 ± 239	1.88	1.96	4.36
PCCS1 857 G354.81–79.56	3.049	–33.228	Cluster candidate	1014 ± 233	1.67	2.23	3.25
PLCKERC857 G257.09–87.10	15.233	–29.122	Cluster candidate	2403 ± 198	3.52	3.02	3.25
PLCKERC857 G014.99–59.64	338.260	–32.139	Cluster candidate	943 ± 115	3.12	1.96	4.36
PLCKERC857 G239.13–78.19	25.333	–31.786	Cluster candidate	1110 ± 145	2.72	1.68	3.25
PLCKERC857 G017.86–68.67	348.790	–30.591	Cluster candidate	1657 ± 167	2.92	3.76	5.05
PLCKERC857 G007.34–65.24	345.366	–35.103	Cluster candidate	920 ± 132	3.32	3.52	3.25
PCCS1 857 G252.98–85.59	16.749	–29.910	Cluster candidate	619 ± 817	1.88	2.76	3.25
PCCS1 857 G058.69+81.03	202.258	30.712	Cluster candidate	845 ± 298	1.45	1.68	4.01
PCCS1 857 G058.53+82.57	200.607	30.124	Cluster candidate	827 ± 197	1.45	2.23	4.36
PLCKERC857 G062.48+78.89	204.276	32.142	Cluster candidate	814 ± 109	0.77	2.50	3.25
PLCKERC857 G063.13+78.00	205.172	32.621	Cluster candidate	912 ± 169	2.10	3.52	3.25
PLCKERC857 G027.36+84.83	198.608	26.510	Cluster candidate	792 ± 93	2.52	3.27	4.01
PLCKERC857 G042.54+81.51	202.358	28.224	Cluster candidate	1697 ± 251	1.67	3.76	4.01
PLCKERC857 G149.81+50.11	158.364	59.196	Cluster candidate	1249 ± 131	5.38	4.47	4.71
PCCS1 857 G089.66+36.10	256.828	60.449	Cluster candidate	886 ± 194	3.32	2.76	2.01
PCCS1 857 G085.48+43.36	244.657	55.771	Cluster candidate	748 ± 128	2.72	3.27	3.64
PLCKERC857 G095.44+58.94	216.128	52.936	Cluster candidate	1141 ± 176	4.65	5.80	2.44
PCCS1 857 G238.20+42.27	150.845	1.469	Cluster candidate	712 ± 269	4.28	3.76	2.01
PLCKERC857 G060.37+66.55	218.579	35.559	Cluster candidate	1241 ± 151	1.00	4.47	5.70
PLCKERC857 G261.89–40.69	70.168	–53.734	Cluster candidate	795 ± 134	3.32	4.47	3.64

Table B2. Candidate protoclusters from the *Planck* 545 GHz catalogues of compact sources. A table containing the properties and identifications of all the *Planck* compact sources is available online.

Name	RA	Dec.	Associations	S_{545} (mJy)	σ_{250}	σ_{350}	σ_{500}
PCCS1 545 G019.76–58.74	337.311	–29.670	Cluster candidate	225 ± 164	2.92	1.68	3.25
PCCS1 545 G354.79–79.57	3.060	–33.226	Cluster candidate	335 ± 158	1.22	1.39	3.25
PLCKERC545 G015.45–60.34	339.084	–31.902	Cluster candidate	607 ± 87	2.72	3.27	4.01
PCCS1 545 G058.72+82.59	200.566	30.136	Cluster candidate	349 ± 161	1.22	1.39	3.64
PCCS1 545 G027.38+84.85	198.581	26.515	Cluster candidate	433 ± 136	1.45	2.23	4.01
PCCS1 545 G084.40+81.05	199.569	33.968	Cluster candidate	387 ± 230	1.88	1.39	3.25
PLCKERC545 G146.77+52.48	164.280	59.031	Cluster candidate	606 ± 73	4.09	4.93	1.06
PCCS1 545 G222.38–54.39	53.046	–27.117	Cluster candidate	182 ± 185	2.10	3.02	2.01
PLCKERC545 G060.36+66.56	218.577	35.554	Cluster candidate	872 ± 114	0.77	4.47	5.70
PLCKERC545 G260.28–39.75	71.996	–52.643	Cluster candidate	471 ± 46	3.71	3.27	3.25

APPENDIX C: PROBABILITY OF N CLUSTER GALAXIES IN M DETECTED SOURCES

For a given protocluster candidate, we observe M sources. Under the assumption that some of these are physically associated with a protocluster, whilst some are not, M is a combination of both the number of field and protocluster galaxies,

$$M = N_{\text{field}} + N_{\text{cluster}}.$$

Furthermore, we assume that the field galaxies are distributed in a Poisson manner, and can be described by Poisson statistics. For a Poisson process with a mean and variance of μ , the probability of observing M sources is given by:

$$\left[\frac{\mu^M}{M!} \right] \exp(-\mu)$$

If we assume that N of our M sources are associated with the protocluster, then $M - N$ sources will be associated with the field, and the probability of observing these $M - N$ field galaxies is:

$$\left[\frac{\mu^{(M-N)}}{(M-N)!} \right] \exp(-\mu)$$

However, this needs to be renormalized as the maximum possible observed field galaxies is now M rather than ∞ (it is impossible to observe $M + 1$ field galaxies out of M total galaxies). This can be done using the Poisson cumulative distribution function, given by:

$$\sum_{i=0}^{i=M} \left[\frac{\mu^i}{i!} \right] \exp(-\mu)$$

where we simply sum over all of the possible arrangements of $N_{\text{field}} + N_{\text{cluster}}$ to give a total of M sources. This is now the correct normalization factor, as it allows for the full range of possibilities stretching from no sources are associated with the protocluster, to all the sources are associated with the protocluster. The full equation becomes:

$$p(NM, \mu) = \frac{\left[\frac{\mu^{(M-N)}}{(M-N)!} \right] \exp(-\mu)}{\sum_{i=0}^{i=M} \left[\frac{\mu^{(i)}}{(i)!} \right] \exp(-\mu)}.$$

Which can be further simplified to:

$$p(NM, \mu) = \frac{\left[\frac{\mu^{(M-N)}}{(M-N)!} \right]}{\sum_{i=0}^{i=M} \left[\frac{\mu^{(i)}}{(i)!} \right]}.$$

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